Package ‘REBayes’

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Title Empirical Bayes Estimation and Inference


Version 1.3

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Depends R (>= 2.10), Matrix

Imports Rmosek, methods, reliaR

Suggests knitr, digest

LazyData TRUE

VignetteBuilder knitr

SystemRequirements MOSEK (http://www.mosek.com) and MOSEK License for use of Rmosek, optional use of the pogs optimizer may require CUDA/GPU accoutrements.

License GPL (>= 2)

URL https://www.r-project.org

NeedsCompilation no

RoxygenNote 6.0.1

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Repository CRAN

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R topics documented:

bball ................................................................. 2
Bmix ................................................................. 3
Description

Data frame consisting of the following variables:

Details

Data is aggregated into half seasons: so season indicates whether the observation is in the first or second half of the season of a given year. Only players who have more than 10 at bats in any half season are included, and only players who have more than three half seasons are represented. The transformed batting average is $arcsin(\sqrt{\frac{H + 1}{4}/(AB + 1/2)})$. Only regular seasons data are included. R programs to extract the data from the original sources are available on request.
Bmix

- Name
- IdNum
- Year
- Halfseason
- Pitcher
- HA transformed batting average;
- AB at bats
- H hits
- BB walks
- YOB Year of Birth;
- age age of the player
- agesq age squared

Source

ESPN Website: http://espn.go.com/mlb/statistics

References


Bmix  Binomial mixture estimation via Kiefer Wolfowitz MLE

Description

Interior point solution of Kiefer-Wolfowitz NPMLE for mixture of binomials

Usage

Bmix(x, k, v = 300, collapse = TRUE, weights = NULL, ...)

Arguments

- x  Count of "successes" for binomial observations
- k  Number of trials for binomial observations
- v  Grid Values for the mixing distribution defaults to equal spacing of length v on [eps, 1-eps], if v is scalar.
- collapse  Collapse observations into cell counts.
- weights  replicate weights for x observations, should sum to 1
- ...  Other arguments to be passed to KWDual to control optimization
Details
The predict method for \texttt{bmiX} objects will compute means, medians or modes of the posterior according to whether the \texttt{Loss} argument is 2, 1 or 0, or posterior quantiles if \texttt{Loss} is in (0,1).

Value
An object of class density with components:

\begin{itemize}
  \item \texttt{x} \quad \text{grid midpoints of evaluation of the mixing density}
  \item \texttt{y} \quad \text{function values of the mixing density at x}
  \item \texttt{g} \quad \text{estimates of the mixture density at the distinct data values}
  \item \texttt{logLik} \quad \text{Log Likelihood value at the estimate}
  \item \texttt{dy} \quad \text{Bayes rule estimates of binomial probabilities for distinct data values}
  \item \texttt{status} \quad \text{exit code from the optimizer}
\end{itemize}

Author(s)
R. Koenker

References


\begin{tabular}{ll}
\texttt{Cosslett} & \textit{Kiefer-Wolfowitz estimator for Cosslett (1983) estimator} \\
\end{tabular}

Description
Kiefer-Wolfowitz-Cosslett estimator for binary response model.

Usage
\begin{verbatim}
Cosslett(x, y, v = 300, weights = NULL, ...)
\end{verbatim}
Arguments

- **x**: is the observed utility difference between two choices, it would be possible to extend this to make \( x \) a linear (index) function of some parameters

- **y**: is the binary outcome

- **v**: the unobserved utility difference taking values on a grid, by default this grid is equally spaced with 300 distinct points, however it is known that the mass points for the problem are located at the data points, \( x \), so users may wish to set \( v = \text{sort}(x) \) although if the sample size is large this can be slow.

- **weights**: replicate weights for \( x \) observations, should sum to 1

... optional parameters to be passed to KWDual to control optimization

Details

In the primal form of the problem the pseudo log likelihood is:

\[
l(f|y) = \sum_i [y_i \log \sum_j (I(v_j \leq x_i) \ast f_j) + (1 - y_i) \log \sum_j (I(v_j > x_i) \ast f_j)]
\]

as usual the implementation used here solves the corresponding dual problem. Cumsum of the output \( y \) gives the CDF of the unobserved utility difference. See the demo(Cosslett1) and demo(Cosslett2) for illustrations without any covariate, and demo(Cosslett3) for an illustration with a covariate using profile likelihood. This model is also known as current status linear regression in the biostatistics literature, see e.g. Groeneboom and Hendrickx (2016) for recent results and references.

Value

an object of class density with the components:

- **x**: points of evaluation of the mixing density

- **y**: function values of the mixing density at \( x \)

- **logL**: log likelihood of estimated model

- **status**: exit code from the optimizer

Author(s)

Jiaying Gu and Roger Koenker

References


**flies**  
**Medfly Data**

**Description**

Medfly data from the Carey et al (1992) experiment. There are 1,203,646 uncensored survival times!

**Usage**

flies

**Format**

A data frame with 19072 observations on the following 17 variables.

- age: age at death in days
- num: frequency count of age at death
- prcurr: current proportion male
- current: current density
- cohort: cohort/pupal batch
- size: pupal size
- cage: cage number
- female: female = 1
- cumul: cumulative density
- prcumu: cumulative proportion male
- begin: initial cage density
- prbegin: initial proportion male
- sizeT: size group 4
- sizeU: size group 5
- sizeV: size group 6
- sizeW: size group 7
- size8: size group 8

**Details**

Quoting from Carey et al (1992) “...Pupae were sorted into one of five size classes using a pupal sorter. This enabled size dimorphism to be eliminated as a potential source of sex-specific mortality differences. Approximately, 7,200 medflies (both sexes) of a given size class were maintained in each of 167 mesh covered, 15 cm by 60 cm by 90 cm aluminum cages. Adults were given a diet of sugar and water, ad libitum, and each day dead flies were removed, counted and their sex determined...”
References


Gammanix

NPMLE for Gamma Mixtures

Description

A Kiefer-Wolfowitz MLE for Gamma mixture models

Usage

Gammanix(x, v = 300, shape = 1, weights = NULL, ...)

Arguments

- x: vector of observed variances
- v: A vector of bin boundaries, if scalar then v equally spaced bins are constructed
- shape: vector of shape parameters corresponding to x
- weights: replicate weights for x observations, should sum to 1
- ...: optional parameters passed to KWDual to control optimization

Value

An object of class density with components:

- x: midpoints of the bin boundaries
- y: estimated function values of the mixing density
- g: function values of the mixture density at the observed x’s.
- logLik: the value of the log likelihood at the solution
- dy: Bayes rule estimates of
- status: the Mosek convergence status.

Author(s)

J. Gu and R. Koenker
References


See Also

Gammamix for a general implementation for Gamma mixtures

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**Description**

Kiefer Wolfowitz Nonparametric MLE for Gaussian Location Mixtures

**Usage**

```r
GLmix(x, v = 300, sigma = 1, hist = FALSE, histm = 300, weights = NULL, ...)
```

**Arguments**

- **x**: Data: Sample Observations
- **v**: Undata: Grid Values defaults equal spacing of with v bins, when v is a scalar
- **sigma**: scale parameter of the Gaussian noise, may take vector values of length(x)
- **hist**: If TRUE then aggregate x to histogram bins, when sigma is vector valued this option is inappropriate unless there are only a small number of distinct sigma values.
- **histm**: histogram bin boundaries, equally spacing with histm bins when scalar.
- **weights**: replicate weights for x observations, should sum to 1
- **...**: other parameters to pass to KWDual to control optimization

**Details**

Kiefer Wolfowitz MLE as proposed by Jiang and Zhang for the Gaussian compound decision problem. The histogram option is intended for large problems, say n > 1000, where reducing the sample size dimension is desirable. When sigma is heterogeneous and hist = TRUE the procedure tries to do separate histogram binning for distinct values of sigma, however this is only feasible when there are only a small number of distinct sigma. By default the grid for the binning is equally spaced on the support of the data. This function does the normal convolution problem, for gamma mixtures of variances see Gvmix, or for mixtures of both means and variances TLvmix.

The predict method for GLmix objects will compute means, medians or modes of the posterior according to whether the loss argument is 2, 1 or 0, or posterior quantiles if loss is in (0,1).
Gompertzmix

Value

An object of class density with components:

- **x**: points of evaluation on the domain of the density
- **y**: estimated function values at the points v, the mixing density
- **g**: the estimated mixture density function values at x
- **logLik**: Log likelihood value at the proposed solution
- **dy**: prediction of mean parameters for each observed x value via Bayes Rule
- **status**: exit code from the optimizer

Author(s)

Roger Koenker

References


Gompertzmix NPMLE for Gompertz Mixtures

Description

Kiefer-Wolfowitz NPMLE for Gompertz Mixtures of scale parameter

Usage

Gompertzmix(x, v = 300, u = 300, alpha, theta, hist = FALSE, weights = NULL, ...)

Arguments

- **x**: Survival times
- **v**: Grid values for mixing distribution
- **u**: Grid values for mixing distribution
- **alpha**: Shape parameter for Gompertz distribution
- **theta**: Scale parameter for Gompertz Distribution
hist If TRUE aggregate to histogram counts
weights replicate weights for x observations, should sum to 1
... optional parameters passed to KWDual to control optimization

Details

Kiefer Wolfowitz NPMLE density estimation for Gompertz scale mixtures. The histogram option is intended for relatively large problems, say n > 1000, where reducing the sample size dimension is desirable. By default the grid for the binning is equally spaced on the support of the data. Parameterization: 
\[ f(t|\alpha,\theta,\nu) = \theta \times \exp(\nu) \times \exp(\alpha \times t) \times \exp(-\theta/\alpha \times \exp(\nu) \times (\exp(\alpha \times t) - 1)) \]

Value

An object of class density with components

- **x**: points of evaluation on the domain of the density
- **y**: estimated function values at the points x, the mixing density
- **logLik**: Log likelihood value at the proposed solution
- **dy**: Bayes rule estimates of theta at observed x
- **status**: exit code from the optimizer

Author(s)

Roger Koenker and Jiaying Gu

References


See Also

Weibullmix

 Gosset Criminal Finger Data

Description

This data was generated by dithering the cell counts in the crimtab available in the base stats package.

Usage

Gosset
Guvenen

Format

A data frame with 3000 observations on 2 variables.

- \texttt{lmfinger}: Length of Left Middle Finger (cm).
- \texttt{kHeight}: \texttt{cm}

Source

see the man page for \texttt{crimtab}

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\begin{tabular}{ll}
Guvenen & \textit{Annual Increments in Log Income} \\
\end{tabular}

Description

Kernel density estimates of the log density of annual increments in log income for U.S. individuals over the period 1994-2013, as estimated by Guvenen.

Usage

Guvenen

Format

A data frame with 279 observations on two variables.

- \texttt{earnings}: annual increment in log income
- \texttt{logdensity}: estimated log density values

Source

**Description**

A Kiefer-Wolfowitz MLE for Gaussian models with independent variances. This can be viewed as a general form for $\chi^2$ mixtures, see Gammamix for a more general form for Gamma mixtures.

**Usage**

```r
GVmix(x, m, v = 300, weights = NULL, ...)
```

**Arguments**

- `x` vector of observed variances
- `m` vector of sample sizes corresponding to `x`
- `v` A vector of bin boundaries, if scalar then `v` equally spaced bins are constructed
- `weights` replicate weights for `x` observations, should sum to 1
- `...` optional parameters passed to KWDual to control optimization

**Value**

An object of class `density` with components:

- `x` midpoints of the bin boundaries
- `y` estimated function values of the mixing density
- `g` function values of the mixture density at the observed x’s.
- `logLik` the value of the log likelihood at the solution
- `dy` Bayes rule estimates of
- `status` the Mosek convergence status.

**Author(s)**

R. Koenker

**References**


**See Also**

Gammamix for a general implementation for Gamma mixtures
**Description**

Interface function for calls to optimizer from various REBayes functions. There are currently two options for the optimization: Mosek (the default) is the original, preferred option and uses interior point methods. It relies on the Rmosek interface to R see installation instructions at https://docs.mosek.com/8.1/rmosek/install-interface.html. A more experimental option employs the pogs package available from https://github.com/foges/pogs and employs an ADMM (Alternating Direction Method of Multipliers) approach.

**Usage**

```r
KWDual(A, d, w, ...)```

**Arguments**

- `A` Linear constraint matrix
- `d` constraint vector
- `w` weights for x should sum to one.
- `...` other parameters passed to control optimization: These may include `rtol` the relative tolerance for dual gap convergence criterion, `verb` to control verbosity desired from mosek, `verb = 0` is quiet, `verb = 5` produces a fairly detailed iteration log, `method` controls the choice of optimizer: by default this is "mosek" which employs interior point methods, however if `method = "pogs"` then optimization is carried out by the ADMM methods described in Fougner and Boyd (2015). This is a first order descent method most suitable for large problems for which parallelization is desirable. For most REBayes applications the default "mosek" method is appropriate and "pogs" should be considered experimental. Note that there is not yet a "pogs" implementation for medde problems. Note also that `method = "pogs"` assumes a distinct control list. Users are responsible for specifying correctly named control variables for each method. The most advantageous implementation of "pogs" requires (CUDA) GPU hardware. `control` is a control list consisting of sublists `iparam`, `dparam`, and `sparam`, containing elements of various mosek control parameters. See the Rmosek and Mosek manuals for further details. A prime example is `rtol` which should eventually be deprecated and folded into `control`, but will persist for a while for compatibility reasons. The default for `rtol` is 1e-6, but in some cases it is desirable to tighten this, say to 1e-10. Another example that motivated the introduction of `control` would be `control = list(iparam = list(num_threads = 1))`, which forces Mosek to use a single threaded process. The default allows Mosek to use multiple threads (cores) if available, which is generally desirable, but may have unintended (undesirable) consequences when running simulations on clusters.
Value

Returns a list with components:

- *f*: dual solution vector, the mixing density
- *g*: primal solution vector, the mixture density evaluated at the data points
- *logLik*: log likelihood
- *status*: return status from Mosek

Author(s)

R. Koenker

References


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### L1norm

#### L1norm for piecewise linear functions

**Description**

Intended to compute the L1norm of the difference between two distribution functions.

**Usage**

```
L1norm(F, G, eps = 1e-06)
```

**Arguments**

- **F**: A stepfunction
- **G**: Another stepfunction
- **eps**: A tolerance parameter
Details

Both F and G should be of class `stepfun`, and they should be non-defective distribution functions. There are some tolerance issues in checking whether both functions are proper distribution functions at the extremes of their support. For simulations it may be prudent to wrap `l1norm` in `try`.

Value

A real number.

Author(s)

R. Koenker

Examples

```r
# Make a random step (distribution) function with Gaussian knots
rstep <- function(n){
  x <- sort(rnorm(n))
  y <- runif(n)
  y <- c(0,cumsum(y)/sum(y))
  stepfun(x,y)
}
F <- rstep(20)
G <- rstep(10)
S <- l1norm(F,G)
plot(F,main = paste("|F - G| = ", round(S,4)))
lines(G,col = 2)
```

Description

Density estimation based on maximum entropy methods

Usage

```r
medde(x, v = 300, lambda = 0.5, alpha = 1, Dorder = 1, w = NULL,
    mass = 1, rtol = 1e-06, verb = 0, control = NULL)
```

Arguments

- `x` Data: either univariate or bivariate, the latter is highly experimental
- `v` Undata: either univariate or bivariate, univariate default is an equally spaced grid of 300 values, for bivariate data there is not (yet) a default.
lambda: total variation penalty parameter, if lambda is in [-1,0], a concavity constraint is imposed. See Koenker and Mizera (2010) for further details on the concavity constrained options.

alpha: Renyi entropy parameter characterizing fidelity criterion by default 1 is log-concave and 0.5 is Hellinger.

Dorder: Order of the derivative operator for the penalty default is $Dorder = 1$, corresponding to TV norm constraint on the first derivative, or a concavity constraint on some transform of the density.

w: weights associated with x,

mass: normalizing constant for fitted density,

rtol: Convergence tolerance for Mosek algorithm,

verb: Parameter controlling verbosity of solution, 0 for silent, 5 gives rather detailed iteration log.

control: Mosek control list see KWDual documentation

Details

See the references for further details. And also Mosek "Manuals". The acronym, according to the urban dictionary has a nice connection to a term used in Bahamian dialect, mostly on the Family Islands like Eleuthera and Cat Island meaning "mess with" "get involved," "get entangled," "fool around," "bother." "I don’t like to medder up with all kinda people" "Don’t medder with people (chirren)" "Why you think she medderin up in their business."

This version implements a class of penalized density estimators solving:

$$\min_x \phi(x_1) |A_1 x_1 - A_2 x_2 = b, 0 \leq x_1, -\lambda \leq x_2 \leq \lambda$$

where $x$ is a vector with two component subvectors: $x_1$ is a vector of function values of the density $x_2$ is a vector of dual values, $\lambda$ is typically positive, and controls the fluctuation of the $Dorder$ derivative of some transform of the density. When alpha = 1 this transform is simply the logarithm of the density, and $Dorder = 1$ yields a piecewise exponential estimate; when $Dorder = 2$ we obtain a variant of Silverman’s (1982) estimator that shrinks the fitted density toward the Gaussian, i.e. with total variation of the second derivative of $\log f$ equal to zero. See demo(Silverman) for an illustration of this case. If $\lambda$ is in $(-1, 0]$ then the $x_2$ TV constraint is replaced by $x_2 \geq 0$, which for $\alpha = 1$, constrains the fitted density to be log-concave; for $\alpha = 0.5$, $-1/\sqrt{T}$ is constrained to be concave; and for $\alpha \leq 0$, $1/f^{\alpha-1}$ is constrained to be concave. In these cases no further regularization of the smoothness of density is required as the concavity constraint acts as regularizer. As explained further in Koenker and Mizera (2010) and Han and Wellner (2016) decreasing $\alpha$ constrains the fitted density to lie in a larger class of quasi-concave densities. See demo(velo) for an illustration of these options, but be aware that more extreme $\alpha$ pose more challenges from an numerical optimization perspective. Fitting for $\alpha < 1$ employs a fidelity criterion closely related to Renyi entropy that is more suitable than likelihood for very peaked, or very heavy tailed target densities. For $\lambda < 0$ fitting for $Dorder = 1$ proceed at your own risk. A closely related problem is illustrated in the demo Brown which imposes a convexity constraint on $0.5x^2 + \log f(x)$. This ensures that the resulting Bayes rule, aka Tweedie formula, is monotone in $x$, as described further in Koenker and Mizera (2013).
Value

An object of class "medde" with components

- \(x\) points of evaluation on the domain of the density
- \(y\) estimated function values at the evaluation points \(x\)
- \(\text{status}\) exit status from Mosek

Author(s)

Roger Koenker and Ivan Mizera

References


See Also

This function is based on an earlier function of the same name in the deprecated package MeddeR that was based on an R-Matlab interface. A plotting method is available, or medde estimates can be added to plots with the usual `lines(meddefit, ...` invocation. For log concave estimates there is also a quantile function `qmedde` and a random number generation function `rmedde`, eventually there should be corresponding functionality for other alphas.

Examples

```r
# Maximum Likelihood Estimation of a Log-Concave Density
set.seed(1968)
x <- rgamma(50, 10)
m <- medde(x, v = 50, lambda = -.5, verb = 5)
plot(m, type = "l", xlab = "x", ylab = "f(x)")
lines(m$x, dgamma(m$x, 10), col = 2)
title("Log-concave Constraint")
```
# Maximum Likelihood Estimation of a Gamma Density with TV constraint

```r
cset.seed(1988)
x <- rgamma(50, 5)
f <- medde(x, v = 50, lambda = 0.2, verb = 5)
plot(f, type = "l", xlab = "x", ylab = "f(x)")
lines(f$x, dgamma(f$x, 5), col = 2)
legend(10, 15, c("ghat", "true"), lty = 1, col = 1:2)
title("Total Variation Norm Constraint")
```

---

**Norberg**

**Norberg Life Insurance Data**

**Description**

Norwegian Life Insurance Exposures and Claims

**Usage**

Norberg

**Format**

A data frame with 72 observations on the following 3 variables.

- `occgroup` Occupational Group
- `exposure` Exposures
- `deaths` Observed Deaths

**Details**

The data arise from 1125 original groups insured during all or part of the period 1982-85 by a major Norwegian insurance company. Exposures can be normalize by a factor of 344 as in Hastrup (2000) and then can be interpreted as the apriori expected number of claims (deaths) for each group. The original 1125 groups were aggregated into 72 as in Norberg (1989).

**References**


plot.medde

Plotting method for medde objects

Description

Plotting method for medde objects

Usage

```r
## S3 method for class 'medde'
plot(x, ...)
```

Arguments

- `x` object obtained from medde fitting
- `...` other parameters to be passed to plot method

Pmix

Poisson mixture estimation via Kiefer Wolfowitz MLE

Description

Poisson mixture estimation via Kiefer Wolfowitz MLE

Usage

```r
Pmix(x, v = 300, exposure = NULL, ...)
```

Arguments

- `x` Data: Sample observations (integer valued)
- `v` Grid Values for the mixing distribution defaults to equal spacing of length v when v is specified as a scalar
- `exposure` observation specific exposures to risk see details
- `...` other parameters passed to KWDual to control optimization

Details

The predict method for Pmix objects will compute means, medians or modes of the posterior according to whether the Loss argument is 2, 1 or 0, or posterior quantiles if Loss is in (0,1).

In the default case exposure = 1 it is assumed that x contains individual observations that are aggregated into count bins via table. When exposure has the same length as x then it is presumed to be individual specific risk exposure and the Poisson mixture is taken to be \( x|v \text{Poi}(v*exposure) \) and the is not aggregated. See for example the analysis of the Norberg data in Koenker and Gu (2016).
Value
An object of class density with components:

- **x** points of evaluation of the mixing density
- **y** function values of the mixing density at x
- **g** function values of the mixture density on 0, 1, \( \ldots, \max(x) + 1 \)
- **logLik** Log Likelihood value at the estimate
- **dy** Bayes rule estimate of Poisson rate parameter at each x
- **status** exit code from the optimizer

Author(s)
Roger Koenker and Jiaying Gu

References


predict.Bmix

**Predict Method for Bmix**

Description
Predict Method for Binomial Mixtures

Usage
```r
## S3 method for class 'Bmix'
predict(object, newdata, Loss = 2, newk, ...)
```

Arguments
- **object** fitted object of class "Bmix"
- **newdata** Values at which prediction is desired
- **Loss** Loss function used to generate prediction: Currently supported values: 2 to get mean predictions, 1 to get median predictions, 0 to get modal predictions or any tau in (0,1) to get tau-th quantile predictions.
- **newk** k values (number of trials) for the predictions
- **...** optional arguments to predict
The predict method for Bmix objects will compute means, quantiles or modes of the posterior according to the loss argument. Typically, newdata would be passed to predict.

A vector of predictions

Jiaying Gu

## Description

Predict Method for Gaussian Location Mixtures

## Usage

```r
## S3 method for class 'GLmix'
predict(object, newdata, Loss = 2, newsigma = NULL, ...)
```

## Arguments

- `object`: fitted object of class "GLmix"
- `newdata`: Values at which prediction is desired
- `Loss`: Loss function used to generate prediction: Currently supported values: 2 to get mean predictions, 1 to get median predictions, 0 to get modal predictions or any tau in (0,1) to get tau-th quantile predictions.
- `newsigma`: sigma values for the predictions
- `...`: optional arguments to predict

The predict method for GLmix objects will compute means, quantiles or modes of the posterior according to the loss argument. Typically, newdata would be passed to predict.

A vector of predictions

Roger Koenker
**predict.Pmix**

Predict Method for Pmix

**Description**

Predict Method for Poisson Mixtures

**Usage**

```r
## S3 method for class 'Pmix'
predict(object, newdata, Loss = 2, newexposure = NULL, ...)
```

**Arguments**

- `object`: fitted object of class "Pmix"
- `newdata`: Values at which prediction is desired
- `Loss`: Loss function used to generate prediction. Currently supported values: 2 to get mean predictions, 1 to get median predictions, 0 to get modal predictions or any tau in (0,1) to get tau-th quantile predictions.
- `newexposure`: exposure values for the predictions
- `...`: optional arguments to predict

**Details**

The predict method for Pmix objects will compute means, quantiles or modes of the posterior according to the Loss argument. Typically, newdata would be passed to predict.

**Value**

A vector of predictions

**Author(s)**

Jiaying Gu
qmedde

Quantile function for medde estimate

Description

Slightly modified version borrowed from the package logcondens Todo: extend this to cases with $\alpha \neq 1$.

Usage

qmedde(p, medde)

Arguments

p vector of probabilities at which to evaluate the quantiles
medde fitted object from medde

rmedde

Random number generation from a medde estimate

Description

Random number generation from a medde estimate

Usage

rmedde(n, medde, smooth = TRUE)

Arguments

n number of observations desired in calls to rmedde
medde fitted medde object for calls in qmedde and rmedde
smooth option to draw random meddes from the smoothed density
Archive function for auxiliary files for latex documents

Description

Creates a tar.gz file with all of the R files needed to recreate the tables and figures that appear in
the paper. Should be considered experimental at this stage. It presumes that tables are generated
with something like the `Hmisc latex` function and included in the latex document with input
commands. Likewise figures are assumed to be included with `includegraphics` and generated
by R in pdf format. This was originally developed to sort out the files for "Empirical Bayesball
Remixed". An optional side of effect of the function to create a tar.gz file with the gzipped R files
required for the paper.

Usage

```r
Rxiv(fname, figures = "figures", tables = "tables", tar = FALSE)
```

Arguments

- `fname` name of the latex file of the paper sans .tex suffix
- `figures` name of the directory with the files for figures
- `tables` name of the directory with the files for tables
- `tar` logical flag, if TRUE generate a gzipped tar file of .R files

Value

a list with the following components

- `rtables` a character array with two columns: .tex files and .R files
- `rfigures` a character array with two columns: .pdf files and .R files
- `rother` a character vector with other R files required.
- `rcached` a character vector with cached Rda files

Author(s)

R. Koenker
tacks

Beckett and Diaconis flipping tacks data

Description

This data was generated by Beckett and Diaconis (1994). They describe it as follows: "The example involves repeated rolls of a common thumbtack. A one was recorded if the tack landed point up and a zero was recorded if the tack landed point down. All tacks started point down. Each tack was flicked or hit with the fingers from where it last rested. A fixed tack was flicked 9 times. The data are recorded in Table 1. There are 320 9-tuples. These arose from 16 different tacks, 2 "flickers," and 10 surfaces. The tacks vary considerably in shape and in proportion of ones. The surfaces varied from rugs through tablecloths through bathroom floors." Following Liu (1996), we treat the data as though they came from 320 independent binomials. See demo(Bmix1) for further details.

Usage

tacks

Format

A data frame with 320 observations on 2 variables.

- x a numeric vector giving the number of tacks landed point up.
- k a numeric vector giving the number of trials.

Source


References


tannenbaum

Perverse Gaussian Mixture data

Description

Gaussian Location Mixture data to illustrate Mosek tolerance problem

Usage

tannenbaum
Format

5000 iid Gaussians This data set was randomly generated in the course of trying to understand some anomalies in estimating Gaussian location mixture problems with GLmix. It is used by demo(tannenbaum) to illustrate that sometimes it is worthwhile to tighten the default convergence tolerance for Mosek.

TLmix

NPMLE for Student t location mixtures

Description

Kiefer Wolfowitz NPMLE for Student t location mixtures

Usage

TLmix(x, v = 300, u = 300, df = 1, hist = FALSE, weights = NULL, ...)

Arguments

x
Data: Sample Observations

v
bin boundaries defaults to equal spacing of length v

u
bin boundaries for histogram binning: defaults to equal spacing

df
Number of degrees of freedom of Student base density

hist
If TRUE then aggregate x to histogram weights

weights
replicate weights for x observations, should sum to 1

... optional parameters passed to KWDual to control optimization

Details

Kiefer Wolfowitz MLE density estimation as proposed by Jiang and Zhang for a Student t compound decision problem. The histogram option is intended for large problems, say n > 1000, where reducing the sample size dimension is desirable. By default the grid for the binning is equally spaced on the support of the data. Equal spaced binning is problematic for Cauchy data.

Value

An object of class density with components:

x
midpoints of evaluation on the domain of the mixing density

y
estimated function values at the points x of the mixing density

logLik
Log likelihood value at the proposed solution

dy
Bayes rule estimates of location at x

status
Mosek exit code
Author(s)
Roger Koenker

References


See Also
GLmix for Gaussian version

Description
Kiefer Wolfowitz NPMLE for Student t non-centrality parameter mixtures Model: 

\[ y_{ig} = \mu_{ig} + e_{ig}, \quad e_{ig} \sim N(0, \sigma_{ig}^2) \]

\( x \) is the vector of t statistics for all groups, which follows t dist if \( \mu_{ig} = 0 \), and noncentral t dist if \( \mu_{ig} \neq 0 \), with \( ncp_g = \mu_{ig}/\sigma_{ig} \). This leads to a mixture of t distribution with \( ncp \) as the mixing parameter. df (degree of freedom) is determined by the group size in the simplest case.

Usage

\[
\text{tncpmix}(x, v = 300, u = 300, df = 1, \text{hist} = \text{FALSE}, \text{weights} = \text{NULL}, \ldots)
\]

Arguments

- **x**: Data: Sample Observations
- **v**: bin boundaries defaults to equal spacing of length \( v \)
- **u**: bin boundaries for histogram binning: defaults to equal spacing
- **df**: Number of degrees of freedom of Student base density
- **hist**: If TRUE then aggregate \( x \) to histogram weights
- **weights**: replicate weights for \( x \) obervations, should sum to 1
- **...**: optional parameters passed to KWDual to control optimization
Value
An object of class density with components:

- **x**: midpoints of evaluation on the domain of the mixing density
- **y**: estimated function values at the points `x` of the mixing density
- **g**: estimated function values at the observed points of mixture density
- **logLik**: Log likelihood value at the proposed solution
- **dy**: Bayes rule estimates of location at `x`
- **status**: Mosek exit code

Author(s)
Roger Koenker

References

See Also
GLmix for Gaussian version

---

**traprule**

Integration by Trapezoidal Rule

**Description**
Integration by Trapezoidal Rule

**Usage**

```
traprule(x, y)
```

**Arguments**

- **x**: points of evaluation
- **y**: function values

**Details**
Crude Riemann sum approximation.
Value

A real number.

Author(s)

R. Koenker

---

**velo**  
*Rotational Velocity of Stars*

Description

A sample of rotational velocities of stars from Hoffleit and Warren (1991) similar to that previously considered by Pal, Woodroofe and Meyer (2007) and used by Koenker and Mizera (2010). The demo(velo) illustrates fitted densities for three relatively weak concavity constraints corresponding to $-1/\sqrt{f}$, $-1/f$ and $-1/f^2$ constrained to be concave. Note that last of these pushes the optimization methods about as far as they can do.

Usage

velo

Format

A numeric vector with 3933 observations on one variable.

- velo: numeric vector with rotational velocities.

Source


References

**Weibullmix**  
*NPMLE for Weibull Mixtures*

**Description**

Kiefer-Wolfowitz NPMLE for Weibull Mixtures of scale parameter

**Usage**

```r
Weibullmix(x, v = 300, u = 300, alpha, lambda = 1, hist = FALSE, weights = NULL, ...)
```

**Arguments**

- `x`: Survival times
- `v`: Grid values for mixing distribution
- `u`: Grid values for histogram bins, if needed
- `alpha`: Shape parameter for Weibull distribution
- `lambda`: Scale parameter for Weibull Distribution; must either have length 1, or length equal to `length(x)` the latter case accommodates the possibility of a linear predictor
- `hist`: If TRUE aggregate to histogram counts
- `weights`: replicate weights for x observations, should sum to 1
- `...`: optional parameters passed to KWDual to control optimization

**Details**

Kiefer Wolfowitz NPMLE density estimation for Weibull scale mixtures. The histogram option is intended for relatively large problems, say n > 1000, where reducing the sample size dimension is desirable. By default the grid for the binning is equally spaced on the support of the data. Parameterization: \( f(t|\alpha, \lambda) = \alpha * \exp(v) * (\lambda * t)^{\alpha-1} * \exp(-(\lambda * t)^\alpha * \exp(v)) \); shape = \( \alpha \); scale = \( \lambda^{-1} * (\exp(v))^{-1/\alpha} \)

**Value**

An object of class density with components

- `x`: points of evaluation on the domain of the density
- `y`: estimated function values at the points x of the mixing density
- `logLik`: Log likelihood value at the proposed solution
- `dy`: Bayes Rule estimates of mixing parameter
- `status`: exit code from the optimizer
Author(s)

Roger Koenker and Jiaying Gu

References


See Also

Gompertzmix

---

Description

A Kiefer-Wolfowitz procedure for ML estimation of a Gaussian model with dependent mean and variance components and weighted longitudinal data. This version assumes a general bivariate distribution for the mixing distribution. The defaults use a rather coarse bivariate gridding.

Usage

```r
WGLVmix(y, id, w, u = SPL, v = SPL, NNN)
```

Arguments

- `y` A vector of observations
- `id` A strata indicator vector of the same length
- `w` A vector of weights
- `u` A vector of bin boundaries for the mean effects
- `v` A vector of bin boundaries for the variance effects
- `...` optional parameters to be passed to KWDual to control optimization

Value

A list consisting of the following components:

- `u` midpoints of mean bin boundaries
- `v` midpoints of variance bin boundaries
- `fuv` the function values of the mixing density.
- `logLik` log likelihood value for mean problem
du Bayes rule estimate of the mixing density means.
dv Bayes rule estimate of the mixing density variances.
status Mosek convergence status

Author(s)

R. Koenker and J. Gu

References


See Also

WTLVmix for an implementation assuming independent heterogeneity

## WGVmix

*WGVmix: Weighted Generalized Maximum Likelihood for Empirical Bayes Estimation of Gamma Variances*

### Description

A Kiefer-Wolfowitz procedure for ML estimation of a Gaussian model with independent variance components with weighted longitudinal data.

### Usage

```r
WGVmix(y, id, w, v, pv = 300, eps = 1e-06, rtol = 1e-06, verb = 0,
       control = NULL)
```

### Arguments

- **y**  
  A vector of observations
- **id**  
  A strata indicator vector of the same length
- **w**  
  A vector of weights
- **v**  
  A vector of bin boundaries for the variance effects
- **pv**  
  The number of variance effect bins, if u is missing
- **eps**  
  A tolerance for determining the support of the bins
- **rtol**  
  A tolerance for determining duality gap convergence tolerance in Mosek
- **verb**  
  A flag indicating how verbose the Mosek output should be
- **control**  
  Mosek control list see KWDual documentation
**WLVMix**

**Details**

See Gu and Koenker (2012?)

**Value**

An object of class 'density' consisting of the following components:

- **x**: the variance bin boundaries
- **y**: the function values of the mixing density for the variances.
- **logLik**: the value of the log likelihood at the solution
- **status**: the mosek convergence status.

**Author(s)**

R. Koenker

**References**


**Description**

A Kiefer-Wolfowitz NPMLE procedure for estimation of a Gaussian model with independent mean and variance prior components with weighted longitudinal data. This version iterates back and forth from Gamma and Gaussian forms of the likelihood.

**Usage**

`WLVMix(y, id, w, u = 300, v = 300, eps = 1e-04, maxit = 2, ...)`

**Arguments**

- **y**: A vector of observations
- **id**: A strata indicator vector indicating grouping of y
- **w**: A vector of weights corresponding to y
- **u**: A vector of bin boundaries for the mean effects
- **v**: A vector of bin boundaries for the variance effects
- **eps**: Convergence tolerance for iterations
- **maxit**: A limit on the number of allowed iterations
- **...**: optional parameters to be passed to KW Dual to control optimization
Value

A list consisting of the following components:

- \( u \)  midpoints of the mean bin boundaries
- \( f_u \)  the function values of the mixing density of the means
- \( v \)  midpoints of the variance bin boundaries
- \( f_v \)  the function values of the mixing density of the variances.
- \( \logLik \)  vector of log likelihood values for each iteration
- \( d_u \)  Bayes rule estimate of the mixing density means.
- \( d_v \)  Bayes rule estimate of the mixing density variances.
- \( \text{status} \)  Mosek convergence status for each iteration

Author(s)

J. Gu and R. Koenker

References


See Also

WGLVmix for a more general bivariate mixing distribution version and WTLVmix for an alternative estimator exploiting a Student/Gamma decomposition

---

**WTLVmix**  
*NPMLE for Longitudinal Gaussian Means and Variances Model*

**Description**

A Kiefer-Wolfowitz NPMLE procedure for estimation of a Gaussian model with independent mean and variance components with weighted longitudinal data. This version exploits a Student t decomposition of the likelihood.

**Usage**

\[
\text{WTLVmix}(y, \ id, \ w, \ u = 300, \ v = 300, \ldots)
\]
Arguments

- **y**: A vector of observations
- **id**: A strata indicator vector indicating grouping of y
- **w**: A vector of weights corresponding to y
- **u**: A vector of bin boundaries for the mean effects
- **v**: A vector of bin boundaries for the variance effects
- **...**: optional parameters to be passed to KWDual to control optimization

Value

A list consisting of the following components:

- **u**: midpoints of the mean bin boundaries
- **fu**: the function values of the mixing density of the means
- **v**: midpoints of the variance bin boundaries
- **fv**: the function values of the mixing density of the variances.
- **logLik**: log likelihood value for mean problem
- **du**: Bayes rule estimate of the mixing density means.
- **dv**: Bayes rule estimate of the mixing density variances.
- **status**: Mosek convergence status

Author(s)

J. Gu and R. Koenker

References


See Also

WGLVmix for a more general bivariate mixing distribution version
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