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R topics documented:

betategarch-package .................................................. 2
coeff.tegarch ........................................................... 3
dST ................................................................. 6
nasdaq ............................................................... 7
predict.tegarch ....................................................... 8
tegarch .............................................................. 10
tegarchLogl .......................................................... 12
tegarchSim .......................................................... 14

Index 17
Simulation, estimation and forecasting of Beta-Skew-t-EGARCH models

Description

This package provides facilities for the simulation, estimation and forecasting of first order Beta-Skew-t-EGARCH models with leverage (one-component and two-component versions), see Harvey and Sucarrat (2014), and Sucarrat (2013).

Let \( y[t] \) denote a financial return at time \( t \) equal to

\[
y[t] = \sigma[t] \cdot \epsilon[t]
\]

where \( \sigma[t] > 0 \) is the scale or volatility (generally not equal to the conditional standard deviation), and where \( \epsilon[t] \) is IID and \( t \)-distributed (possibly skewed) with \( \text{df} \) degrees of freedom. Then the first order log-volatility specification of the one-component Beta-Skew-t-EGARCH model can be parametrised as

\[
\sigma[t] = \exp(\lambda[t]), \\
\lambda[t] = \omega + \lambda[dagger], \\
\lambda[dagger][t] = \phi1 * \lambda[dagger][t-1] + \kappa1 * u[t-1] + \kappastar * \text{sign}[-y] * (u[t-1]+1).
\]

So the scale or volatility is given by \( \sigma[t] = \exp(\lambda[t]) \). The \( \omega \) is the unconditional or long-term log-volatility, \( \phi1 \) is the GARCH parameter (\(|\phi1| < 1 \) implies stability), \( \kappa1 \) is the ARCH parameter, \( \kappastar \) is the leverage or volatility-asymmetry parameter and \( u[t] \) is the conditional score or first derivative of the log-likelihood with respect to \( \lambda \). The score \( u[t] \) is zero-mean and IID, and \( (u[t]+1)/(\text{df}+1) \) is Beta distributed when there is no skew in the conditional density of \( \epsilon[t] \). The two-component specification is given by

\[
\sigma[t] = \exp(\lambda[t]), \\
\lambda[t] = \omega + \lambda1[dagger] + \lambda2[dagger], \\
\lambda1[dagger][t] = \phi1 * \lambda[dagger][t-1] + \kappa1 * u[t-1], \\
\lambda2[dagger][t] = \phi2 * \lambda[dagger][t-1] + \kappa2 * u[t-1] + \kappastar * \text{sign}[-y] * (u[t-1]+1).
\]

The first component, \( \lambda1[dagger] \), is interpreted as the long-term component, whereas the second component, \( \lambda2[dagger] \), is interpreted as the short-term component.

Details

Package: betategarch
Type: Package
Version: 3.3
Date: 2016-10-16
License: GPL-2
LazyLoad: yes

The two main functions of the package are \texttt{tegarchSim} and \texttt{tegarch}. The first simulates a Beta-Skew-t-EGARCH models whereas the second estimates one. The second object returns an object (a
list) of class 'tegarch', and a collection of methods can be applied to this class: `coef.tegarch`, `fitted.tegarch`, `logLik.tegarch`, `predict.tegarch`, `print.tegarch`, `residuals.tegarch`, `summary.tegarch` and `vcov.tegarch`. In addition, the output produced by the `tegarchSim` function and the `fitted.tegarch` and `residuals.tegarch` methods are of the `Z's` ordered observations (`zoo`) class, which means a range of time-series methods are available for these objects.

Author(s)

Genaro Sucarrat, [http://www.sucarrat.net/](http://www.sucarrat.net/)

References


Harvey and Sucarrat (2014), 'EGARCH models with fat tails, skewness and leverage'. Computational Statistics and Data Analysis 76, pp. 320-338.


Examples

```r
# simulate 500 observations from model with default parameter values:
set.seed(123)
y <- tegarchSim(500)

# estimate and store as 'mymod':
mymod <- tegarch(y)

# print estimates and standard errors:
print(mymod)

# graph of fitted volatility (conditional standard deviation):
plot(fitted(mymod))

# plot forecasts of volatility 1-step ahead up to 10-steps ahead:
plot(predict(mymod, n.ahead=10))
```

Description

Extraction methods for objects of class 'tegarch' (i.e. the result of estimating a Beta-Skew-t-EGARCH model)
Usage

```r
## S3 method for class 'tegarch'
coef(object, ...)  
## S3 method for class 'tegarch'
fitted(object, verbose = FALSE, ...)  
## S3 method for class 'tegarch'
logLik(object, ...)  
## S3 method for class 'tegarch'
print(x, ...)  
## S3 method for class 'tegarch'
residuals(object, standardised = TRUE, ...)  
## S3 method for class 'tegarch'
summary(object, verbose = FALSE, ...)  
## S3 method for class 'tegarch'
vcov(object, ...)  
```

Arguments

- `object`: an object of class 'tegarch'
- `x`: an object of class 'tegarch'
- `verbose`: logical. If FALSE (default) then only basic information is returned
- `standardised`: logical. If TRUE (default) then the standardised residuals are returned. If FALSE then the scaled (by sigma) residuals are returned
- `...`: additional arguments

Details

Empty

Value

- `coef`: A numeric vector containing the parameter estimates
- `fitted`: A zoo object. If verbose=FALSE (default), then the zoo object is a vector containing the fitted conditional standard deviations. If verbose = TRUE, then the zoo object is a matrix containing the return series y, fitted scale (sigma), fitted conditional standard deviation (stdev), fitted log-scale (lambda), dynamic component(s) (lambdadagger in the 1-component specification, lambda1dagger and lambda2dagger in the 2-component specification), the score (u), scaled residuals (epsilon) and standardised residuals (residstd)
- `logLik`: The value of the log-likelihood at the maximum
- `print`: Prints the most important parts of the estimation results
- `residuals`: A zoo object. If standardised = TRUE (default), then the zoo object is a vector with the standardised residuals. If standardised = FALSE, then the zoo vector contains the scaled residuals
- `summary`: A list. If verbose = FALSE, then only the most important entries are returned. If verbose = TRUE, then all entries apart from the 1st. (the y series) is returned
v cov: The variance-covariance matrix of the estimated coefficients. The matrix is obtained by inverting the numerically estimated Hessian.

Author(s)
Genaro Sucarrat, http://www.sucarrat.net/

References

Harvey and Sucarrat (2014), 'EGARCH models with fat tails, skewness and leverage'. Computational Statistics and Data Analysis 76, pp. 320-338.


See Also
tegarch, coef, fitted, logLik, predict, predict.tegarch, print, summary, vcov

Examples
# simulate 500 observations from model with default parameter values:
set.seed(123)
y <- tegarchsim(500)
# estimate and store as 'mymodel':
mymod <- tegarch(y)
# print estimation result:
print(mymod)
# extract coefficients:
coef(mymod)
# extract log-likelihood:
logLik(mymod)
# plot fitted conditional standard deviations:
predict(mymod)
# plot all the fitted series:
plot(fitted(mymod, verbose=TRUE))
# histogram of standardised residuals:
hist(residuals(mymod))
**The skewed t distribution**

**Description**
Density, random number generation, mean, variance, skewness and kurtosis functions for the uncentred skewed t distribution. The skewing method is that of Fernandez and Steel (1998).

**Usage**

```r
dST(y, df = 10, sd = 1, skew = 1, log = FALSE)
rSt(n, df = 10, skew = 1)
StMean(df, skew = 1)
StVar(df, skew = 1)
StSkewness(df, skew = 1)
StKurtosis(df, skew = 1)
```

**Arguments**

- `y`: numeric vector of quantiles
- `n`: integer, the number of observations
- `df`: degrees of freedom, greater than 0 and less than Inf
- `sd`: scale, greater than 0 and less than Inf
- `skew`: skewness, greater than 0 and less than Inf. Symmetry obtains when `skew = 1` (default).
- `log`: logical. TRUE returns the natural log of the density value, FALSE (default) returns the density value.

**Details**
Empty

**Value**

- `dST`: a numeric value, either the density value or the natural log of the density value
- `rSt`: a numeric vector with n random numbers
- `StMean`: The mean of an uncentred skewed t variable
- `StVar`: The variance of an uncentred skewed t variable
- `StSkewness`: 3rd. moment of a standardised skewed t variable
- `StKurtosis`: 4th. moment of a standardised skewed t variable

**Note**
Empty
Author(s)

Genaro Sucarrat, http://www.sucarrat.net/

References


See Also

tegarchSim

Examples

```r
# Generate 1000 random numbers from the skewed t:
set.seed(123)
eps <- rSt(500, df=5) # symmetric t
eps <- rSt(500, df=5, skew=0.8) # skewed to the left
eps <- rSt(500, df=5, skew=2) # skewed to the right

# Compare empirical mean with analytical:
mean(eps)
StMean(5, skew=2)

# Compare empirical variance with analytical:
var(eps)
StVar(5, skew=2)
```

### nasdaq

*Daily Apple stock returns*

Description

The dataset contains two variables, day and nasdaqret. Day is the date of the return and nasdaqret is the daily (closing value) log-return in percent of the Apple stock over the period 10 September 1985 - 10 May 2011 (a total of 6835 observations).

Usage

data(nasdaq)

Format

A data frame with 3215 observations:

day a factor

nasdaqret a numeric vector
The data is studied in more detail in Harvey and Sucarrat (2014), and in Sucarrat (2013).

The source of the original raw data is http://yahoo.finance.com/.

Harvey and Sucarrat (2014), 'EGARCH models with fat tails, skewness and leverage'. Computational Statistics and Data Analysis 76, pp. 320-338.

Examples

data(nasdaq) #load data into workspace
mymod <- tegarch(nasdaq[,"nasdaqret"])[estimate volatility model of Apple returns
print(mymod)

predict.tegarch Generate volatility forecasts n-steps ahead

Description
Generates volatility forecasts from a model fitted by tegarch (i.e. a Beta-Skew-t-EGARCH model)

Usage

## S3 method for class 'tegarch'
predict(object, n.ahead = 1, initial.values = NULL, n.sim = 10000,
verbose = FALSE, ...)

Arguments

object an object of class 'tegarch'.
n.ahead the number of steps ahead for which prediction is required.
initial.values a vector containing the initial values of lambda and lambdadagger (lambda1dagger
and lambda2dagger for 2-component models). If NULL (default) then the fitted
values associated with the last return-observation are used
n.sim number of simulated skew t variates.
verbose logical. If FALSE (default) then only the conditional standard deviations are
returned. If TRUE then also the scale is returned.
... additional arguments
Details

The forecast formulas of exponential ARCH models are much more complicated than those of ordinary or non-exponential ARCH models. This is particularly the case when the conditional density is skewed. The forecast formula of the conditional scale of the Beta-Skew-t-EGARCH model is not available in closed form. Accordingly, some terms (expectations involving the skewed t) are estimated numerically by means of simulation.

Value

A zoo object. If verbose = FALSE, then the zoo object is a vector with the forecasted conditional standard deviations. If verbose = TRUE, then the zoo object is a matrix with forecasts of both the conditional scale and the conditional standard deviation

Author(s)

Genaro Sucarrat, http://www.sucarrat.net/

References


Harvey and Sucarrat (2014), 'EGARCH models with fat tails, skewness and leverage'. Computational Statistics and Data Analysis 76, pp. 320-338.


See Also
tegarch, predict

Examples

```r
# simulate series with 500 observations:
set.seed(123)
y <- tegarchSim(500, omega=0.01, phi1=0.9, kappa1=0.1, kappastar=0.05, df=10, skew=0.8)

# estimate a 1st. order Beta-t-EGARCH model and store the output in mymod:
mymod <- tegarch(y)

# plot forecasts of volatility 1-step ahead up to 10-steps ahead:
plot(predict(mymod, n.ahead=10))
```
Estimate first order Beta-Skew-t-EGARCH models

**Description**

Fits a first order Beta-Skew-t-EGARCH model to a univariate time-series by exact Maximum Likelihood (ML) estimation. Estimation is via the `nlminb` function.

**Usage**

```r
tegarch(y, asym = TRUE, skew = TRUE, components = 1, initial.values = NULL,
lower = NULL, upper = NULL, hessian = TRUE, lambda.initial = NULL,
c.code = TRUE, logl.penalty = NULL, aux = NULL, ...)
```

**Arguments**

- `y` numeric vector, typically a financial return series.
- `asym` logical. TRUE (default) includes leverage or volatility asymmetry in the log-scale specification.
- `skew` logical. TRUE (default) enables and estimates the skewness in conditional density (epsilon). The skewness method is that of Fernandez and Steel (1998).
- `components` Numeric value, either 1 (default) or 2. The former estimates a 1-component model, the latter a 2-component model.
- `initial.values` NULL (default) or a vector with the initial values. If NULL, then the values are automatically chosen according to model (with or without skewness, 1 or 2 components, etc.).
- `lower` NULL (default) or a vector with the lower bounds of the parameter space. If NULL, then the values are automatically chosen.
- `upper` NULL (default) or a vector with the upper bounds of the parameter space. If NULL, then the values are automatically chosen.
- `hessian` logical. If TRUE (default) then the Hessian is computed numerically via the `optimHess` function. Setting hessian=FALSE speeds up estimation, which might be particularly useful in simulation. However, it also slows down the extraction of the variance-covariance matrix by means of the `vcov` method.
- `lambda.initial` NULL (default) or a vector with the initial value(s) of the recursion for lambda and lambdadagger. If NULL then the values are chosen automatically.
- `c.code` logical. TRUE (default) is faster since it makes use of compiled C-code.
- `logl.penalty` NULL (default) or a numeric value. If NULL then the log-likelihood value associated with the initial values is used. Sometimes estimation can result in NA and/or +/-Inf values, which are fatal for simulations. The value logl.penalty is the value returned by the log-likelihood function in the presence of NA or +/-Inf values.
- `aux` NULL (default) or a list, se code. Useful for simulations (speeds them up).
- `...` further arguments passed to the `nlminb` function.
Value

Returns a list of class `tegarch` with the following elements:

- `y`: the series used for estimation.
- `date`: date and time of estimation.
- `initial.values`: initial values used in estimation.
- `lower`: lower bounds used in estimation.
- `upper`: upper bounds used in estimation.
- `lambda.initial`: initial values of lambda provided by the user, if any.
- `model`: type of model estimated.
- `hessian`: the numerically estimated Hessian.
- `sic`: the value of the Schwarz (1978) information criterion.
- `par`: parameter estimates.
- `objective`: value of the log-likelihood at the maximum.
- `convergence`: an integer code. 0 indicates successful convergence, see the documentation of `nlminb`.
- `iterations`: number of iterations, see the documentation of `nlminb`.
- `evaluations`: number of evaluations of the objective and gradient functions, see the documentation of `nlminb`.
- `message`: a character string giving any additional information returned by the optimizer, or NULL. For details, see PORT documentation and the `nlminb` documentation.
- `note`: an additional message returned if one tries to estimate a 2-component model without leverage.

Note

Empty

Author(s)

Genaro Sucarrat, [http://www.sucarrat.net/](http://www.sucarrat.net/)

References


Harvey and Sucarrat (2014), 'EGARCH models with fat tails, skewness and leverage'. Computational Statistics and Data Analysis 76, pp. 320-338.
tegarchLogl


See Also
tegarchSim, coef.tegarch, fitted.tegarch, logLik.tegarch, predict.tegarch, print.tegarch, residuals.tegarch, summary.tegarch, vcov.tegarch

Examples

```r
# simulate series with 500 observations:
set.seed(123)
y <- tegarchSim(500, omega=0.01, phi1=0.9, kappa1=0.1, kappastar=0.05,
                 df=10, skew=0.8)

# estimate a 1st. order Beta-t-EGARCH model and store the output in mymod:
mymod <- tegarch(y)

# print estimates and standard errors:
print(mymod)

# graph of fitted volatility (conditional standard deviation):
plot(fitted(mymod))

# graph of fitted volatility and more:
plot(fitted(mymod, verbose=TRUE))

# plot forecasts of volatility 1-step ahead up to 20-steps ahead:
plot(predict(mymod, n.ahead=20))

# full variance-covariance matrix:
vcov(mymod)
```

tegarchLogl  

Auxiliary functions

Description

tegarchLogl, tegarchLogl2, tegarchRecursion and tegarchRecursion2 are auxiliary functions called by tegarch, and which are not intended to be used for the average user. Henceforth they are thus only scarcely documented, but most should either be self-explanatory (for the non-average user!) or more or less documented in relation with the tegarch and tegarchSim functions.
Usage

```r
# the '2' relates to the 2-component specification:
tegarchLogl(y, pars, lower = -Inf, upper = Inf, lambda.initial = NULL,
          logl.penalty = -1e+100, c.code = TRUE, aux = NULL)
tegarchLogl2(y, pars, lower = -Inf, upper = Inf, lambda.initial = NULL,
          logl.penalty = -1e+101, c.code = TRUE, aux = NULL)
tegarchRecursion(y, omega = 0.1, phi1 = 0.4, kappa1 = 0.2, kappastar = 0.1,
                  df = 10, skew = 0.6, lambda.initial = NULL, c.code = TRUE, verbose = FALSE,
                  aux = NULL)
tegarchRecursion2(y, omega = 0.1, phi1 = 0.4, phi2 = 0.2, kappa1 = 0.05,
                   kappa2 = 0.1, kappastar = 0.02, df = 10, skew = 0.6, lambda.initial = NULL,
                   c.code = TRUE, verbose = FALSE, aux = NULL)
```

Arguments

- `y` numeric vector, typically a financial return series
- `omega` numeric
- `phi1` numeric, must be less than 1 in absolute value
- `phi2` numeric, must be less than 1 in absolute value
- `kappa1` numeric
- `kappa2` numeric
- `kappastar` numeric
- `df` numeric, the value of df (degrees of freedom)
- `skew` numeric (positive), the value of skew (skewness parameter)
- `verbose` logical. If FALSE (default) then only lambda is returned. If TRUE then a matrix
  with `y` and the fitted values of, amongst other, sigma, the log-scale (lambda), the
  conditional standard deviation (stdev), `u`, epsilon and the standardised residuals
  (residstd) are returned
- `pars` numeric vector, the parameter values
- `lower` numeric vector, the lower bounds used during estimation
- `upper` numeric vector, the upper bounds used during estimation
- `lambda.initial` NULL (default) or initial value(s) of the recursion for lambda. If NULL, then
  the values are chosen automatically
- `logl.penalty` numeric value
- `c.code` logical. TRUE (default) is faster since it makes use of compiled C-code
- `aux` NULL (default) or a list, see `tegarch` code

Details

tegarchLogl and tegarchLogl2 return the value of the log-likelihood for a 1-component and 2-
component model, respectively.
**Value**

- `tegarchLog1`: The log-likelihood value (i.e. a numeric) of a 1-component specification
- `tegarchLog2`: The log-likelihood value (i.e. a numeric) of a 2-component specification
- `tegarchRecursion`: A numeric vector containing the lambda values if `verbose=FALSE` (default). If `verbose=TRUE` then a matrix then a matrix with y and the fitted values of sigma, the log-scale (lambda), the conditional standard deviation (stdev), u, epsilon and the standardised residuals (residstd) are returned.
- `tegarchRecursion2`: A numeric vector containing the lambda values if `verbose=FALSE` (default). If `verbose=TRUE`, then a matrix then a matrix with y and the fitted values of sigma, the log-scale (lambda), the conditional standard deviation (stdev), u, epsilon and the standardised residuals (residstd) are returned.

**Author(s)**

Genaro Sucarrat, http://www.sucarrat.net/

**References**


Harvey and Sucarrat (2014), 'EGARCH models with fat tails, skewness and leverage'. Computational Statistics and Data Analysis 76, pp. 320-338.


**See Also**

- `tegarch`, `tegarchSim`, `fitted.tegarch`

---

**tegarchSim**

*Simulate from a first order Beta-Skew-t-EGARCH model*

**Description**

Simulate the y series (typically interpreted as a financial return or the error in a regression) from a first order Beta-Skew-t-EGARCH model. Optionally, the conditional scale (sigma), log-scale (lambda), conditional standard deviation (stdev), dynamic components (lambdadagger in the 1-component specification, lambda1dagger and lambda2dagger in the 2-component specification), score (u) and centred innovations (epsilon) are also returned.
**Usage**

tegarchSim(n, omega = 0, phi1 = 0.95, phi2 = 0, kappa1 = 0.01, kappa2 = 0, kappastar = 0, df = 10, skew = 1, lambda.initial = NULL, verbose = FALSE)

**Arguments**

- **n** integer, length of y (i.e. no of observations)
- **omega** numeric, the value of omega
- **phi1** numeric, the value of phi1
- **phi2** numeric, the value of phi2
- **kappa1** numeric, the value of kappa1
- **kappa2** numeric, the value of kappa2
- **kappastar** numeric, the value of kappastar
- **df** numeric, the value of df (degrees of freedom)
- **skew** numeric, the value of skew (skewness parameter)
- **lambda.initial** NULL (default) or initial value(s) of the recursion for lambda or log-volatility. If NULL then the values are chosen automatically
- **verbose** logical, TRUE or FALSE (default). If TRUE then a matrix with n rows containing y, sigma, lambda, lambdadagger, u and epsilon is returned. If FALSE then only y is returned

**Details**

Empty

**Value**

A **zoo** vector of length n or a **zoo** matrix with n rows, depending on the value of verbose.

**Author(s)**

Genaro Sucarrat, [http://www.sucarrat.net/](http://www.sucarrat.net/)

**References**


Harvey and Sucarrat (2014), 'EGARCH models with fat tails, skewness and leverage'. Computational Statistics and Data Analysis 76, pp. 320-338.

See Also
tegarch, zoo

Examples

```r
# 1-component specification: simulate series with 500 observations:
set.seed(123)
y <- tegarchSim(500, omega=0.01, phi1=0.9, kappa1=0.1, kappastar=0.05,
    df=10, skew=0.8)

# simulate the same series, but with more output (volatility, log-volatility or
# lambda, lambdadagger, u and epsilon)
set.seed(123)
y <- tegarchSim(500, omega=0.01, phi1=0.9, kappa1=0.1, kappastar=0.05, df=10, skew=0.8,
    verbose=TRUE)

# plot the simulated values:
plot(y)

# 2-component specification: simulate series with 500 observations:
set.seed(123)
y <- tegarchSim(500, omega=0.01, phi1=0.95, phi2=0.9, kappa1=0.01, kappa2=0.05,
    kappastar=0.03, df=10, skew=0.8)
```
Index

*Topic Statistical Models
  coef.tegarch, 3
  dST, 6
  predict.tegarch, 8
  tegarch, 10
  tegarchLogl, 12
  tegarchSim, 14
*Topic datasets
  nasdaq, 7
betategarch (betategarch-package), 2
betategarch-package, 2
  coef, 5
  coef.tegarch, 3, 3, 12
  dST, 6
  fitted, 5
  fitted.tegarch, 3, 12, 14
  fitted.tegarch (coef.tegarch), 3
  logLik, 5
  logLik.tegarch, 3, 12
  logLik.tegarch (coef.tegarch), 3
  nasdaq, 7
  nlminb, 10
  predict, 5, 9
  predict.tegarch, 3, 5, 8, 12
  print, 5
  print.tegarch, 3, 12
  print.tegarch (coef.tegarch), 3
  residuals.tegarch, 3, 12
  residuals.tegarch (coef.tegarch), 3
  rST (dST), 6
  STkurtosis (dST), 6
  STmean (dST), 6
  STskewness (dST), 6
  STvar (dST), 6
  summary, 5
  summary.tegarch, 3, 12
  summary.tegarch (coef.tegarch), 3
  tegarch, 2, 5, 8, 9, 10, 12–14, 16
  tegarchLogl, 12
  tegarchLogl2 (tegarchLogl), 12
  tegarchRecursion (tegarchLogl), 12
  tegarchRecursion2 (tegarchLogl), 12
  tegarchSim, 2, 3, 7, 12, 14, 14
  vcov, 5
  vcov.tegarch, 3, 12
  vcov.tegarch (coef.tegarch), 3
  zoo, 3, 15, 16