Package ‘bvls’

Type Package
Title The Stark-Parker algorithm for bounded-variable least squares
Version 1.4
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Description An R interface to the Stark-Parker implementation of an
algorithm for bounded-variable least squares
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bvls-package

The Stark-Parker algorithm for bounded-variable least squares

Description

An R interface to the Stark-Parker implementation of an algorithm for bounded-variable least
squares that solves \[ \min \| Ax - b \|_2 \] with the constraint \[ l \leq x \leq u, \] where \[ l, x, u \in \mathbb{R}^n, b \in \mathbb{R}^m \]
and \( A \) is an \( m \times n \) matrix.

References

tational Statistics, 10, 129-141.
See Also

`bvls`, the method "L-BFGS-B" for `optim`, `solve.QP`, `nnls`

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**bvls**

*The Stark-Parker implementation of bounded-variable least squares*

**Description**

An R interface to the Stark-Parker implementation of bounded-variable least squares that solves the least squares problem

\[
\min \| Ax - b \|_2 \text{ with the constraint } l \leq x \leq u, \text{ where } l, x, u \in \mathbb{R}^n, b \in \mathbb{R}^m
\]

and \( A \) is an \( m \times n \) matrix.

**Usage**

`bvls(A, b, bl, bu, key=0, istate=rep(0, ncol(A)+1))`

**Arguments**

- \( A \) numeric matrix with \( m \) rows and \( n \) columns
- \( b \) numeric vector of length \( m \)
- \( bl \) numeric vector of length \( n \) specifying the lower bound on each element of \( x \)
- \( bu \) numeric vector of length \( n \) specifying the upper bound on each element of \( x \)
- \( key \) If \( key > 0 \) the routine initializes using the user’s guess about which components of \( x \) are active, i.e. are strictly within their bounds, which are at their lower bounds, and which are at their upper bounds. This information is supplied through the array \( istate \).
- \( istate \) vector of length \( ncol(A)+1 \). If \( key > 0 \), \( istate \) is as follows: the last contains the total number of components at their bounds (the bound variables). The absolute values of the first \( nbound \leftarrow \text{tail}(istate,1) \) entries of \( istate \) are the indices of these bound components of \( x \). The sign of \( istate[1:nbound] \) indicates whether \( x(\text{abs}(istate[1:nbound])) \) is at its upper or lower bound. \( istate[1:nbound] \) is positive if the component is at its upper bound, negative if the component is at its lower bound. \( istate[(nbound+1):ncol(A)] \) contain the indices of the components of \( x \) that are active (i.e. are expected to lie strictly within their bounds). When \( key > 0 \), the routine initially sets the active components to the averages of their upper and lower bounds.

**Value**

`bvls` returns an object of class "bvls".

The generic assessor functions `coefficients`, `fitted.values`, `deviance` and `residuals` extract various useful features of the value returned by `bvls`.

An object of class "bvls" is a list containing the following components:

- \( x \) the parameter estimates.
deviance  the residual sum-of-squares.
residuals  the residuals, that is response minus fitted values.
fitted     the fitted values.

Source

This is an R interface to the Fortran77 code accompanying the article referenced below by Stark PB, Parker RL (1995), and distributed via the statlib on-line software repository at Carnegie Mellon University (URL http://lib.stat.cmu.edu/general/bvls). The code was modified slightly to allow compatibility with the gfortran compiler. The authors have agreed to distribution under GPL version 2 or newer.

References


See Also

the method "L-BFGS-B" for optim, solve.QP, nnls

Examples

```r
## simulate a matrix A
## with 3 columns, each containing an exponential decay
t <- seq(0, 2, by = .04)
k <- c(.5, .6, 1)
A <- matrix(nrow = 51, ncol = 3)
Acolfunc <- function(k, t) exp(-k*t)
for(i in 1:3) A[,i] <- Acolfunc(k[i], t)

## simulate a matrix X
X <- matrix(nrow = 50, ncol = 3)
wavenum <- seq(18000, 28000, length=nrow(X))
location <- c(25000, 22000)
delta <- c(1000, 1000)
Xcolfunc <- function(wavenum, location, delta)
  exp(- log(2) * (2 * (wavenum - location)/delta)^2)
for(i in 1:2) X[,i] <- Xcolfunc(wavenum, location[i], delta[i])
X[1:40,3] <- Xcolfunc(wavenum, 23000, 1000)[11:nrow(X)]
X[41:nrow(X),3] <- Xcolfunc(wavenum, 23000, 1000)[21:30]

## set seed for reproducibility
set.seed(3300)

## simulated data is the product of A and X with some
## spherical Gaussian noise added
matdat <- A %*% t(X) + .005 * rnorm(nrow(A) * nrow(X))
```
## estimate the rows of X using BVLS criteria

```r
vls_sol <- function(matdat, A) {
  X <- matrix(0, nrow = ncol(matdat), ncol = ncol(A))
  bu <- c(Inf, Inf, .75)
  bl <- c(0, 0, -.75)
  for(i in 1:ncol(matdat))
    X[,i] <- coef(vls(A, matdat[,i], bl, bu))
  X
} 
X_vlsls <- vlsSol(matdat, A)
```

```r
matplot(X, type="p", pch=20)
matplot(X_vlsls, type="l", pch=20, add=TRUE)
legend(10, -.5,
  c("bound <= zero", "bound <= zero", "bound <= -.75 <= .75"),
  col = c(1,2,3), lty=c(1,2,3),
  text.col = "blue")
```

## Not run:

## can solve the same problem with L-BFGS-B algorithm
## but need starting values for x

```r
bfgs_sol <- function(matdat, A) {
  startval <- rep(0, ncol(A))
  fn1 <- function(par, b, A) sum((b - A %*% par)^2)
  X <- matrix(0, nrow = ncol(matdat), ncol = 3)
  bu <- c(1000, 1000, .75)
  bl <- c(0, 0, -.75)
  for(i in 1:ncol(matdat))
    X[,i] <- optim(startval, fn = fn1, b=matdat[,i], A=A, upper = bu, lower = bl,
                   method="L-BFGS-B")$par
  X
} 
X_bfgs <- bfgsSol(matdat, A)
```

## the RMS deviation under BVLS is less than under L-BFGS-B
```r
sqrt(sum((X - X_vlsls)^2)) < sqrt(sum((X - X_bfgs)^2))
```

## and L-BFGS-B is much slower
```r
system.time(vlsSol(matdat, A))
system.time(bfgsSol(matdat, A))

## End(Not run)
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