Package ‘fdaMixed’

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Type Package

Title Functional Data Analysis in a Mixed Model Framework

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Description Likelihood based analysis of 1-dimension functional data in a mixed-effects model framework. Matrix computation are approximated by semi-explicit operator equivalents with linear computational complexity.

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Description

Likelihood based analysis of 1-dimension functional data in a mixed-effects model framework. The methodology is designed for equidistantly sampled high frequency data, where the needed matrix computation may be approximated by semi-explicit operator equivalents with linear computational complexity. Extensions exist for non-equidistantly sampled data, but these have not been implemented.

Details

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Type: Package
Version: 0.5
Date: 2017-03-07
License: GPL-2
LazyLoad: yes

Author(s)

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References


See Also

Implementation done using the package RcppArmadillo. For penalized likelihood analysis of functional data see the packages fda and fda.usc.

Examples

```r
x <- seq(0,2*pi,length.out=200)
y.true <- sin(x)+x
y.obs <- y.true + rnorm(200)
est0 <- fdaLm(y.obs~0,Fright="open",right=2*pi)
```
dataTrans

Scale invariant Box-Cox transformation

Description

Performs forward and backward Box-Cox power transformation including the invariance scaling based on the geometric mean.

Usage

```
dataTrans(y, mu, direction = "backward", geoMean = NULL)
```

Arguments

- **y**: The numeric variable object to be transformed.
- **mu**: The power parameter, where zero corresponds to the logarithmic transformation.
- **direction**: A character variable. If the lower case of the first letter equals "b" (default), then the backward transformation is performed. If the lower case of the first letter equals "f", then the forward transformation is performed.
- **geoMean**: If a numeric is stated, then this is taken as the geometric mean of the untransformed observations. If NULL (default), then the geometric mean is computed from the observation \( y \). The latter is only available for the forward transformation.

Value

The transformed variable.

Note

This function is intended to be used in conjunction with \texttt{fdaLm} to achieve estimates on the original scale. Thus, the geometric mean of the original observations should be kept in order to have the correct backtransformation.

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Examples

```r
# Make 3 samples with the following characteristics:
# 1) length N=500
# 2) sinusoid form + linear fixed effect + noise
# 3) exponential transformed
# ---------------------------------------------

N <- 500
sample.time <- seq(0, 2*pi, length.out = N)
z <- c("a", "b", "c")
x0 <- c(0, 10, 20)
x1 <- rep(x0, each = N)
y <- c(sin(sample.time), sin(sample.time), sin(sample.time)) + x1 + rnorm(3 * N)

# Make exponential-Box-Cox-backtransformation
# Scaling with geometric mean requires that we solve the Whiteker function
geoMean <- mean(y)
geoMean <- uniroot(function(x)(x * log(x) - geoMean), c(exp(-1), (1 + geoMean)^2))$root
y <- dataTrans(y, 0, "b", geoMean)

# ---------------------------------------------
# Do fda's with global and marginal fixed effects
# Also seek to find Box-Cox transformation with mu=0
# ---------------------------------------------
est0 <- fdaLm(y | z ~ x0, boxcox = 1)
est1 <- fdaLm(y | z ~ x1, boxcox = 1)

# ---------------------------------------------
# Display results
# ---------------------------------------------

# Panel 1
plot(sample.time, dataTrans(est0$betaHat[, "(Intercept)"] + est0$betaHat[, "x0"],
est0$boxcoxHat, "b", geoMean)/
dataTrans(est0$betaHat[, "(Intercept)"], est0$boxcoxHat, "b", geoMean),
main = "Effect of x (true=1.2)", xlab = "time",
ylab = "response ratio")
abline(h = dataTrans(est1$betaHat[, "(Intercept)"] + est1$betaHat[, "x1"],
est1$boxcoxHat, "b", geoMean)/
dataTrans(est1$betaHat[, "(Intercept)"], est1$boxcoxHat, "b", geoMean), col = 2)
legend("topleft", c("marginal", "global"), pch = c(1, NA), lty = c(NA, 1), col = 1:2)

# Panel 2
plot(sample.time, dataTrans(est0$betaHat[, "(Intercept)"] + est0$betaHat[, "x0"],
est0$boxcoxHat, "b", geoMean)/
dataTrans(est0$betaHat[, "(Intercept)"], est0$boxcoxHat, "b", geoMean),
main = "Effect of x (true=1)",
xlab = "time",
ylab = "response difference")
abline(h = dataTrans(est1$betaHat[, "(Intercept)"] + est1$betaHat[, "x1"],
est1$boxcoxHat, "b", geoMean)
dataTrans(est1$betaHat["(Intercept)"], est1$boxcoxHat, "b", geoMean), col=2)
legend("bottomleft", c("marginal", "global"), pch=c(1,NA), lty=c(NA,1), col=1:2)

# Panel 3
plot(sample.time, est0$xBLUP[,1], type="l",
main="Marginal ANOVA", xlab="time", ylab="x BLUP")

# Panel 4
plot(sample.time, est1$xBLUP[,1], type="l",
main="Global ANOVA", xlab="time", ylab="x BLUP")
Start value for the lambda parameter describing the L-operator. Presently the following forms are implemented: If K.order is odd, then lambda may have length=1 corresponding to $L=\text{lambda}[1]*D^\text{K.order}$, or length=2 corresponding to $L=\text{lambda}[1]*D^\text{2*K.order}+\text{lambda}[2]$. If K.order is even, then lambda may have length=1 corresponding to $L=\text{lambda}[1]*D^\text{2*K.order}$, length=2 corresponding to $L=\text{lambda}[1]*D^\text{2*K.order}+\text{lambda}[2]*D^\text{K.order}$, or length=3 corresponding to $L=\text{lambda}[1]*D^\text{2*K.order}+\text{lambda}[2]*D^\text{K.order}+\text{lambda}[3]$. Used depending on nlSearch as described above. All coefficients must be non-negative, and the leading coefficient lambda[1] must be strictly positive. Coefficients equal to zero are kept fixed at zero in the non-linear optimization.

If TRUE (default), then a non-linear optimization of the parameters boxcox, G, lambda is performed (present implementation uses nlminb). If FALSE, then the initial values of the non-linear parameters are used.

The order of the K-operator.

The requested order of derivatives of the prediction of the serial correlated effect xBLUP. If NULL (default), then D.order is set to the maximal recommended order K.order.

Specification of the K.order boundary conditions at the left limit of the sampling interval. Value "tied" (default) gives bridge-type conditions. Value "open" shifts up the bridge-type conditions one differential order, hence removing the restriction on the level (corresponding to the open end of a Brownian motion). Otherwise arbitrary linear boundary conditions may be specified as a matrix with dimension (K.order,2*K.order).

Similarly for the K.order boundary conditions at the right limit of the sampling interval.

Left limit of the sampling interval. If NULL (default), then left is set to 0.

Right limit of the sampling interval. If NULL (default), then right is set to the number of sampling points. Thus, the default values of left and right give sampling distance equal to 1.

The response variable Y is taken from the data frame data (subsidiary the parent environment). If there is more than one sample, then the responses must be stacked sample-wise on top of each other. The sample identifier id is sought for in both data frames data and design (subsidiary the parent environment). The primarily function of the identifier is to decide the number of samples. But if id is present in both data frames, and if there is more that one sample, then this variable is also used to match the reponse vector to the design variables (i.e. these need not appear in the same order).

The design variables fixed and random for the fixed and the random effects are taken from the data frame design (subsidiary the parent environment), subsidiary from the data frame data (subsidiary the parent environment).

If the number of observations in the design variables equal the total number of response observations, then a global ANOVA is performed. If the number of observations in the design variables equal the number of sample points, then a marginal ANOVA is performed.
Value

A list with components

- `logLik`: Minus twice the log restricted likelihood taken at the estimates.
- `ANOVA`: Specifies whether fixed and random effects were estimated globally (global) or marginally (marginal).
- `n1Search`: Specifies whether non-linear optimization was performed (TRUE / FALSE).
- `counts`: Number of computations of the negative log likelihood.
- `boxcoxHat`: Maximum restricted likelihood estimate for the power parameter in the scale invariant Box-Cox transformation. Equal to not done if the Box-Cox transformation is not used.
- `Ghat`: Maximum restricted likelihood estimate for the variance matrix of the random effects.
- `lambdaHat`: Maximum restricted likelihood estimate for the lambda parameter describing the L-operator.
- `sigma2hat`: Maximum restricted likelihood estimate for the noise variance.
- `betaHat`: For global ANOVA a vector with estimate for the fixed effect. For marginal ANOVA a matrix with estimate for the fixed effects.
- `uBLUP`: For global ANOVA a vector with prediction of the random effect. For marginal ANOVA a matrix with predictions of the random effects.
- `xBLUP`: Array with predictions of serial correlated effects. The dimension is (sample length, sample numbers, 1+D.order).
- `condRes`: Matrix of conditional residuals. The dimension is (sample length, sample numbers).
- `betaVar`: Variance matrix of fixed effect estimate.

Note

- If the real value of the left most eigenvalues are non-positive, and if the real value of the right most eigenvalues are non-negative, then the underlying algorithm is numerical stable. This will always be the situation for the present restriction of the L-operator.
- If lambda has length=1, then it may also be interpreted as the smoothing parameter in the penalized likelihood framework.
- If D.order is chosen larger than K.order, this number of derivatives are also computed during the non-linear optimization. This might slow down the computation speed a little bit.

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See Also

See also `findRoots` and `dataTrans`.
findRoots

Complex roots of quadratic polynomial

Description

Find complex roots of polynomials in x that are quadratic polynomials in x^k

Usage

findRoots(coefs, k = 1)

Arguments

coefs  Coefficients (c_0, c_k, c_2k) of quadratic polynomial in x^k. Also accepts matrix input (J,3).
k  Order of x^k
Details

It is assumed that $c_{-2k}$ is non-zero, and that at least one of $c_0$ and $c_k$ are non-zero (otherwise, we have a double root, which is not treated by \texttt{fdalm} in the present implementation). An error is issued if these assumptions are violated.

Value

A list with components

- \texttt{left} \quad The k roots with left most real components
- \texttt{right} \quad The k roots with right most real components

Note

This function is intended for internal usage in \texttt{fdalm} to find eigenvalues. If a robust and stable method of finding all the complex roots is a polynomial were available, then this could be used in \texttt{fdalm} instead enhancing the scope of this function.

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References


Examples

\begin{verbatim}
findRoots(c(-1,0,1),1)
findRoots(c(1,-1,1),2)
\end{verbatim}
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