rv: a simulation-based random variable class
Version 2.3.0
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1 Introduction

rv is an implementation of a simulation-based random variable object class for R, originally introduced in Kerman and Gelman [2007].

rv implements a new class of vectors that contain a ‘hidden dimension’ of simulations in each scalar component. These rv objects can be manipulated much like any numeric vectors, but the arithmetic operations are performed on the simulations, and summaries are calculated from the simulation vectors.

rv is convenient for manipulating posterior simulations obtained from MCMC samplers, for example using Umacs [Kerman, 2006] or R2WinBUGS [Sturtz et al., 2005] (the package provides a coercion method to convert bugs objects to rv objects.)

The paper by Kerman and Gelman [2007] introduces the principles of the design of random variable objects. This document is a short overview of some of the commands provided by the package rv. At the end of the document there is a short description of the implementation.

1.1 Installation

Install the package ‘rv’ (version 2.1.1 or higher) using the Package Installer command in R (from the menu), and load the package using,

```R
> library(rv)
```
2 A quick tour

The rv objects (or, “random vectors”) that we manipulate usually come from a Markov chain sampler. To introduce some commands quickly, we will instead use some random vectors generated by random-vector generating functions which sample directly from a given (standard) distribution.

Number of simulations. First, we will set the number of simulations we use. We choose 4000 simulations per each scalar component of a random vector:

\[
> \text{setnsims}(4000)
\]

\[
[1] 4000
\]

We will not usually change this value during our session, unless we want to repeat our analysis with more (or fewer) simulations. The default value is 4000, set whenever the package is loaded for the first time in the workspace; therefore this is not strictly a necessary step to do every time we start the package.

A Normally distributed random vector. To draw a random Gaussian (Normal) vector of length 5 with corresponding means 1, 2, 3, 4, 5 and s.d. 1,

\[
> x \leftarrow \text{rvnorm}(\text{mean}=1:5, \text{sd}=1)
\]

In effect, the object \(x\) now contains five vectors of length 4000, drawn (internally) using \texttt{rnorm}, but we see \(x\) as a vector of length 5.

The length of the vector is derived from the length of the mean vector (and the sd vector), and it is not necessary to specify a parameter “\(n\)”.

Quick distribution summary. To summarize the distribution of \(x\) by viewing quantiles, means, and s.d.’s, we only type the name of the object at the console:

\[
> x
\]

\[
\begin{array}{cccccccccccc}
\text{mean} & \text{sd} & 1\% & 2.5\% & 25\% & 50\% & 75\% & 97.5\% & 99\% & \text{sims} \\
[1] & 0.98 & 0.98 & -1.35 & -0.926 & 0.31 & 1 & 2.9 & 3.2 & 4000 \\
[2] & 1.98 & 1.01 & -0.40 & 0.015 & 1.28 & 2 & 2.7 & 3.9 & 4.3 & 4000 \\
[3] & 3.02 & 0.99 & 0.76 & 1.059 & 2.35 & 3 & 3.7 & 5.0 & 5.2 & 4000 \\
[4] & 4.02 & 1.01 & 1.64 & 1.983 & 3.35 & 4 & 4.7 & 5.9 & 6.3 & 4000 \\
[5] & 4.99 & 0.97 & 2.77 & 3.144 & 4.33 & 5 & 5.7 & 6.9 & 7.2 & 4000 \\
\end{array}
\]
Similarly we can draw from Poisson (rvpois) Gamma, (rvgamma), Binomial (rvbinom):

```r
> y <- rvpois(lambda=10)
```

**Componentwise summaries.** To extract the means, we use rvmean, the s.d.’s, we use rvsd, the minimum, rvmin, the maximum rvmax, and the quantiles, we use rvquantile. The componentwise medians are also obtained by rvmedian:

```r
> rvmean(x)
[1] 0.98 1.98 3.02 4.02 4.99
> rvsd(x)
[1] 0.98 1.01 0.99 1.01 0.97
> rvquantile(x, c(0.025,0.25,0.5,0.75,0.975))
   2.5%   25%   50%   75%   98%
[1,] -0.926 0.31   1.7 1.7  2.9
[2,] 0.015 1.28  2.7 2.7  3.9
[3,] 1.059 2.35  3.7 3.7  5.0
[4,] 1.983 3.35  4.7 4.7  5.9
[5,] 3.144 4.33  5.7 5.7  6.9
> rvmedian(x)
[1] 1 2 3 4 5
> rvmin(y)
[1] 1
> rvmax(y)
[1] 24
```

For convenience, there is an alias E(...) for rvmean(...) which gives the “expectation” of a random vector.

**Note.** Since the random vectors are all represented by simulations, the expectation and all other functions that we compute are just numerical approximations. Generating a “standard normal random variable” with `z <- rvnorm(n=1, mean=0, sd=1)` will not have an expectation exactly zero. Our main purpose here is to handle simulations, so the answers will be approximate and necessarily involve a simulation error.
Extracting and replacing. Since rv objects work just like vectors, we can extract and replace components by using the bracket notation. Here we replace the 3rd and 4th components with random variables having (an approximate) binomial distributions:

```r
> x[3:4] <- rvbinom(size=1, prob=c(0.1, 0.9))
> x[3:4]
         mean      sd     1%     2.5%   25%   50%   75%   97.5%   99%   sims
[1] 0.1000 0.3000 0.0000 0.0000 0.00 0.00 0.00 0.0000 0.00 4000
[2] 0.9000 0.3100 0.0000 0.0000 1.00 1.00 1.00 1.0000 1.00 4000
```

The “mean” column now shows the estimate of the expectation of the two indicator functions we generated.

Imputing into regular vectors. To “impute” a random vector in a regular numeric vector, we can either first turn the constant vector into an rv object:

```r
> y <- as.rv(1:5)
> y
         mean      sd     1%     2.5%   25%   50%   75%   97.5%   99%   sims
[1] 1.0000 0.0000 1.0000 1.0000 1.00 1.00 1.00 1.0000 1.00 1
[2] 2.0000 0.0000 2.0000 2.0000 2.00 2.00 2.00 2.0000 2.00 1
[3] 0.1000 0.3000 0.0000 0.0000 0.00 0.00 0.00 1.0000 0.00 4000
[4] 0.9000 0.3100 0.0000 0.0000 1.00 1.00 1.00 1.0000 1.00 4000
[5] 5.0000 0.0000 5.0000 5.0000 5.00 5.00 5.00 5.0000 5.00 1
```

or, use the special function `impute` that can handle regular vectors and rv objects:

```r
> y <- (1:5)
> impute(y, 3:4) <- x[3:4]
> y
         mean      sd     1%     2.5%   25%   50%   75%   97.5%   99%   sims
[1] 1.0000 0.0000 1.0000 1.0000 1.00 1.00 1.00 1.0000 1.00 1
[2] 2.0000 0.0000 2.0000 2.0000 2.00 2.00 2.00 2.0000 2.00 1
[3] 0.1000 0.3000 0.0000 0.0000 0.00 0.00 0.00 1.0000 0.00 4000
[4] 0.9000 0.3100 0.0000 0.0000 1.00 1.00 1.00 1.0000 1.00 4000
[5] 5.0000 0.0000 5.0000 5.0000 5.00 5.00 5.00 5.0000 5.00 1
The non-random components appearing as “constants,” or in other words, random variables with point-mass distributions (and therefore having a zero variance).

**Summaries of functions of random vectors.** Standard numerical functions can be applied directly to random vectors. To find a summary of the distribution of the function \(1/(1 + \exp(-x_1))\), we would write,

```r
> 1/(1+exp(-x[1]))
```

```
mean    sd   1%   2.5%  25%  50%  75%  97.5% 99%  sims
[1]  0.69 0.18 0.21 0.28 0.58 0.73 0.84  0.95 0.96 4000
```

Or of the function of almost anything we like:

```r
> 2*log(abs(x[2]))
```

```
mean    sd   1%   2.5%  25%  50%  75%  97.5% 99%  sims
[1]  1.0  1.5 -4.4 -2.9  0.5  1.4  2.0  2.7  2.9 4000
```

**Order statistics.** To simulate the order statistics of a random vector \(x\), we can use `sort(x), min(x), max(x)`.

```r
> x <- rpois(lambda=1:5)
> x
```

```
mean    sd   1%   2.5%  25%  50%  75%  97.5% 99%  sims
[1]  0.98 1.0  0    0   0  1   2   3   4 4000
[2]  1.98 1.4  0    0   1  2   3   5   6 4000
[3]  2.97 1.7  0    0   2  3   4   7   8 4000
[4]  4.02 2.0  1    3   4   5   8   9  10 4000
[5]  5.03 2.2  1    3   5   6  10  11  11 4000
```

```r
> sort(x)
```

```
mean    sd   1%   2.5%  25%  50%  75%  97.5% 99%  sims
[1]  0.61 0.69  0    0   0  1   2   2   2 4000
[2]  1.62 0.91  0    0   1  2   3   3   4 4000
[3]  2.72 1.07  1    2   3   3   5   5   5 4000
[4]  4.02 1.29  2    3   4   5   7   7   7 4000
[5]  5.96 1.83  3    5   6   7  10  11  11 4000
```

```r
> min(x)
```

```r
> 1/(1+exp(-x[1]))
```

```r
> 2*log(abs(x[2]))
```
Random matrices and arrays.  

`rv` objects behave like numerical vectors in R; thus you can set their dimension attributes to make them appear as arrays, and also use the matrix multiplication operator. (Note: `%**%` performs the matrix multiplication, ensuring that non-rv and `rv` objects get properly multiplied. Using `%*%` does not work if the matrix or vector on the left is not an rv object.)

```r
> p <- runif(4) # Some prior probabilities.
> y <- rvbinom(size=1, prob=p) # y is now a rv of length 4.
> dim(y) <- c(2,2) # Make y into a 2x2 matrix.
> y
```

```
mean   sd  1%  2.5%  25%  50%  75%  97.5%  99%  sims
[1,1]  0.3435 0.47 0 0 0 0 1 1 1 4000
[2,1]  0.1010 0.30 0 0 0 0 1 1 1 4000
[1,2]  0.4225 0.49 0 0 0 0 1 1 1 4000
[2,2]  0.0065 0.08 0 0 0 0 0 0 0 4000
```

```r
> y %**% y
```

```
mean   sd  1%  2.5%  25%  50%  75%  97.5%  99%  sims
[1,1]  0.385  0.51 0 0 0 0 1 1 2 4000
[2,1]  0.032  0.18 0 0 0 0 1 1 1 4000
[1,2]  0.147  0.36 0 0 0 0 1 1 1 4000
[2,2]  0.048  0.21 0 0 0 0 1 1 1 4000
```

The componentwise summary functions such as `E(rvmean)` and `rvsd` return the summaries with the correct dimension attribute set:

```r
> E(y)
```

```
[,1]  [,2]
[1,] 0.34 0.4225
[2,] 0.10 0.0065
```
Creating indicator functions with logical operations. Applying logical operations gives indicators of events. If \( z \) is a standard normal random variable the indicator of the event \( \{ z > 1 \} \) is given by the statement \( z > 1 \):

```r
> z <- rnorm(1)
> z > 1

mean  sd 1% 2.5% 50% 75% 97.5% 99% sims
[1] 0.14 0.35 0 0 0 0 1 1 4000
```

We can also use the convenience function \( \text{Pr}(\ldots) \) to compute the estimates of the expectation of these indicators:

```r
> Pr(z > 1)
[1] 0.14
```

Of course, we can find joint events as well and compute their probabilities similarly. To find the probability that \( Z_1 > Z_2^2 \), where both \( Z_1 \) and \( Z_2 \) are independent standard normal, we’d type

```r
> z <- rnorm(2)
> Pr(z[1] > z[2]^2)
[1] 0.28
```

We can even compute probabilities of intersections or unions of events,

```r
[1] 0.022
[1] 0.2
```

Functions of several random variables. We can use random vectors, regular vectors, standard elementary functions, logical operations in any combination as we wish.

Example. Let \( z_1, z_2 \) be standard normal, and let \( y_1 = \exp(z_1), y_2 = y_1 \exp(z_2) \). Compute the expectation of \( x = (y_1 - 1)1_{y_1>1}1_{y_2>1} \) and find the probability \( \text{Pr}(x > 1) \).
> z <- rnorm(n=2, mean=0, sd=1)
> y <- exp(z)
> E(x)
[1] 0.79
> Pr(x>1)
[1] 0.22

**Posterior simulations from a classical regression model.** We can generate posterior simulations from a classical regression model, using the standard assumptions for the priors. For convenience there is a function `posterior` to do this.

> n <- 10
> ## Some covariates
> X <- data.frame(x1=rnorm(n, mean=0), x2=rpois(n, 10) - 10)
> y.mean <- (1.0 + 2.0 * X$x1 + 3.0 * X$x2)
> y <- rnorm(n, y.mean, sd=1.5) ## n random numbers
> D <- cbind(data.frame(y=y), X)
> ## Regression model fit
> fit <- lm(y ~ x1 + x2, data=D)
The Bayesian estimates (posterior distributions) are represented by,

> Post <- posterior(fit)
> Post

$\texttt{$beta$}$

<table>
<thead>
<tr>
<th>name</th>
<th>mean</th>
<th>sd</th>
<th>1%</th>
<th>2.5%</th>
<th>25%</th>
<th>50%</th>
<th>75%</th>
<th>97.5%</th>
<th>99%</th>
<th>sims</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Intercept)</td>
<td>1.1</td>
<td>0.80</td>
<td>-0.91</td>
<td>-0.45</td>
<td>0.56</td>
<td>1.0</td>
<td>1.5</td>
<td>2.7</td>
<td>3.1</td>
<td>4000</td>
</tr>
<tr>
<td>x1</td>
<td>2.0</td>
<td>0.71</td>
<td>0.19</td>
<td>0.57</td>
<td>1.58</td>
<td>2.0</td>
<td>2.4</td>
<td>3.4</td>
<td>3.8</td>
<td>4000</td>
</tr>
<tr>
<td>x2</td>
<td>2.9</td>
<td>0.22</td>
<td>2.33</td>
<td>2.43</td>
<td>2.77</td>
<td>2.9</td>
<td>3.0</td>
<td>3.3</td>
<td>3.4</td>
<td>4000</td>
</tr>
</tbody>
</table>

$\texttt{$sigma$}$

<table>
<thead>
<tr>
<th>mean</th>
<th>sd</th>
<th>1%</th>
<th>2.5%</th>
<th>25%</th>
<th>50%</th>
<th>75%</th>
<th>97.5%</th>
<th>99%</th>
<th>sims</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.7</td>
<td>0.54</td>
<td>0.91</td>
<td>0.97</td>
<td>1.3</td>
<td>1.6</td>
<td>1.9</td>
<td>3</td>
<td>3.5</td>
<td>4000</td>
</tr>
</tbody>
</table>
Creating replicated simulations. Continuing the previous example, we’ll resample from the sampling distribution of \( y \) using the posterior simulations we got. We can use the function `rvnorm` to do this, since it accepts *random vectors as arguments*. Rather than think `rvnorm` to draw normal random vectors, it rather “samples from the normal model.” The vector will be normal *given* (constant) mean and s.d., but if the mean and s.d. are not constants, the resulting vector will not be normal.

```r
> sigma <- Post$sigma
> betas <- Post$beta
> M <- model.matrix(fit)
> y.rep <- rvnorm(mean=M %*% betas, sd=sigma)
> mlplot(y.rep) # Summarize graphically.
```

Note also that `sigma` is also an rv object.

The matrix multiplication statement returns a random vector of length 10:

```r
> M %*% betas

<table>
<thead>
<tr>
<th>name</th>
<th>mean</th>
<th>sd</th>
<th>1%</th>
<th>2.5%</th>
<th>25%</th>
<th>50%</th>
<th>75%</th>
<th>97.5%</th>
<th>99%</th>
<th>sims</th>
</tr>
</thead>
<tbody>
<tr>
<td>[2]</td>
<td>2</td>
<td>-2.95</td>
<td>1.24</td>
<td>-6.1</td>
<td>-5.4</td>
<td>-3.7</td>
<td>-3.0</td>
<td>-2.20</td>
<td>-0.41</td>
<td>0.18</td>
</tr>
<tr>
<td>[3]</td>
<td>3</td>
<td>-0.41</td>
<td>1.19</td>
<td>-3.3</td>
<td>-2.7</td>
<td>-1.1</td>
<td>-0.4</td>
<td>0.27</td>
<td>2.05</td>
<td>2.61</td>
</tr>
<tr>
<td>[4]</td>
<td>4</td>
<td>-1.34</td>
<td>1.00</td>
<td>-3.7</td>
<td>-3.3</td>
<td>-1.9</td>
<td>-1.3</td>
<td>-0.76</td>
<td>0.76</td>
<td>1.20</td>
</tr>
<tr>
<td>[5]</td>
<td>5</td>
<td>7.99</td>
<td>0.56</td>
<td>6.6</td>
<td>6.9</td>
<td>7.6</td>
<td>8.0</td>
<td>8.33</td>
<td>9.14</td>
<td>9.41</td>
</tr>
<tr>
<td>[6]</td>
<td>6</td>
<td>8.49</td>
<td>0.62</td>
<td>6.9</td>
<td>7.3</td>
<td>8.1</td>
<td>8.5</td>
<td>8.86</td>
<td>9.76</td>
<td>10.12</td>
</tr>
<tr>
<td>[8]</td>
<td>8</td>
<td>-1.63</td>
<td>0.91</td>
<td>-3.8</td>
<td>-3.4</td>
<td>-2.2</td>
<td>-1.6</td>
<td>-1.08</td>
<td>0.24</td>
<td>0.76</td>
</tr>
<tr>
<td>[9]</td>
<td>9</td>
<td>8.53</td>
<td>0.63</td>
<td>7.0</td>
<td>7.3</td>
<td>8.2</td>
<td>8.5</td>
<td>8.91</td>
<td>9.82</td>
<td>10.18</td>
</tr>
<tr>
<td>[10]</td>
<td>10</td>
<td>22.25</td>
<td>1.33</td>
<td>18.7</td>
<td>19.4</td>
<td>21.5</td>
<td>22.3</td>
<td>23.05</td>
<td>24.90</td>
<td>25.40</td>
</tr>
</tbody>
</table>
```

Thus all the uncertainty in the mean estimate \( X\beta \) and the residual s.d. estimate \( \sigma \) is propagated when the replicated vector \( y^{rep} \) is generated. In effect, this single line of code thus will in fact draw from the distribution

\[
p(y^{rep}|y) = \int \int \text{Normal}(y^{rep}|\mu,\sigma)p(\mu,\sigma|y)d\mu d\sigma.
\]

For convenience, there is a generic method `rvpredict` to generate replications and predictions:

```r
> ## Replications
> y.rep <- rvpredict(fit)
```
We can also generate predictions at some other covariate values:

```r
## Predictions at the mean of the covariates
X.pred <- data.frame(x1=mean(X$x1), x2=mean(X$x2))
y.pred <- rvpredict(fit, newdata=X.pred)
```

We can also perturb (add uncertainty to) the covariate `x1`, then predict again.

```r
X.rep <- X
X.rep$x1 <- rnorm(n=n, mean=X.rep$x1, sd=sd(X.rep$x1))
y.pred2 <- rvpredict(fit, newdata=X.rep)
y.pred2
```

```
mean  sd 1% 2.5% 25% 50% 75% 97.5% 99% sims
[1] 13.143 2.1 8.1 8.9 11.833 13.134 14.4 17.56 18.7 4000
[2] -2.326 2.0 -7.5 -6.3 -3.556 -2.333 -1.1 1.65 2.6 4000
[3] 1.479 2.4 -4.5 -3.4 0.024 1.508 3.0 6.05 7.1 4000
[4] 0.053 2.1 -5.3 -4.4 -1.213 0.037 1.4 4.34 5.3 4000
[6] 7.907 1.8 3.4 4.2 6.778 7.895 9.0 11.70 12.5 4000
[8] -4.792 2.6 -11.1 -9.8 -6.347 -4.801 -3.3 0.39 1.9 4000
[9] 7.426 1.9 2.4 3.6 6.296 7.472 8.6 10.93 12.0 4000
```

**Graphical summaries** Graphical summaries are still in development, but it is now possible to plot a scatterplot with a regular vector against a random vector, showing the 50% and 95% uncertainty intervals along with the median, using `plot(y,x,...)`, where `y` is not random but `x` is. or we can show two random scalars plotted as a 2-dimensional scatterplot with `plot(x[1],x[2],...)`.

To illustrate, let us plot the predicted intervals of the previous example, along with the data points.

Plot the predictions against `y` in red color; then plot the perturbed predictions with blue color.

```r
## Plot predictions
plot.rv(D$y, y.rep, rvcol="red")
points.rv(D$y + 0.33, y.pred2, rvcol="blue")
```
Note that the function method needs to be called explicitly to be able to plot constants vs. rv objects. If the first argument of `plot(x, ...)` is an rv object, one can call `plot`.

Or, we can show a random vectors as horizontal intervals using `mlplot`:

```r
> mlplot(y.rep, rvcol="red")
> mlplot(D$y, add=TRUE, col="blue", pch="x")
```
A histogram of the simulations of a random scalar \( x[1] \), can be plotted with `rvhist`:

```r
> rvhist(rvnorm(mean=0, sd=1)^3, xlim=c(-3, 3), col="red", main="Cubed standard normal")
```
Example: Simulating Pólya’s Urn. This code simulates 200 iterations of the well-known Pólya’s urn problem. The parameter \( x/(n+1) \) for the Bernoulli-variate-generating function \( \text{rvbern}(\ldots) \) is random: we can generate random variables using random parameters without much trickery; our code looks therefore more natural.

The model:

\[
X_0 = 1 \quad \text{(1)}
\]

\[
X_n - X_{n-1} | X_{n-1} \sim \text{Bernoulli}(X_{n-1}/(n+1)) \quad \text{(2)}
\]

The R code:

```r
> x <- 1
> for (n in 1:100) {
+   x <- x + rvbern(n=1, prob=x / (n + 1))
+ }
```
> rvhist(x / (n + 1)) # Histogram

We can see that the distribution is close to uniform, which is the limiting distribution in this case.

3 Details

Obtaining the simulation matrix. To extract the simulation matrix embedded in an rv object, use `sims`:

```r
> s <- sims(y.rep)
> dim(s)
[1] 4000 10
```

It is our convention to have the columns represent the random vector and the rows represent the draws from the joint distribution of the vector.
Converting matrices and vectors of simulations to rv objects. A matrix or a vector of simulations is converted into an rv object by \texttt{rvsims}. Continuing the above example, we’ll convert the matrix back to an rv object.

\begin{verbatim}
> y <- rvsims(s)
\end{verbatim}

You can verify that \texttt{all(sims(y)==s)} returns TRUE. Also note that \texttt{length(y)} gives 10, since \texttt{y} is “just a vector.”

Coercing vectors and matrices. The function \texttt{as.rv(x)} coerces objects to rv objects. However, this does not mean that matrices of simulations are turned into rv objects—this is done with \texttt{rvsims}, as explained above. \texttt{as.rv(rnorm(4000))} would return a random vector of length 4000, where each component has zero variance (and one single simulation). You probably mean \texttt{rvsims(rnorm(4000))}, but the correct way to generate this object is \texttt{rvnorm(1)}.

Obtaining simulations from R2WinBUGS R2WinBUGS [Sturtz et al., 2005] is an interface for calling WinBUGS within R, and obtaining the simulations as an R matrix (that is embedded in a “bugs” object). If \texttt{bugsobj} is the bugs object returned by the \texttt{bugs(...)} function call, then \texttt{as.rv} will coerce it into a list of random vectors, split by the parameter names: \texttt{y <- as.rv(bugsobj)}

Obtaining simulations from Umacs. Umacs facilitates the construction of a Gibbs/Metropolis sampler in R [Kerman, 2006], and returns the simulations wrapped in an “UmacsRun” object. Again, the coercion method \texttt{as.rv} will convert the Umacs object, say \texttt{obj}, into a list of named random vectors: \texttt{y <- as.rv(obj)}.

4 Some implementation details

\texttt{rv} is written in “S3” style object-oriented R rather than using the \texttt{methods} (“S4”) package. The main reason was speed, the secondary consideration was the ease of writing new functions.

The main class is called \texttt{rv}. Most functions expecting an rv object have names starting with \texttt{rv}. For example, \texttt{rvnorm}, \texttt{rvmean}, etc.
The package also features rv-specific methods extending the basic numeric vector classes, e.g. `c.rv, plot.rv`, etc. However, the method dispatch in R will not call the `rv` class method if the first object in the argument list is not an `rv` object; for example, `c(...)` will not call `c.rv` in the following case: suppose that `x` is an object of class `rv` and `k <- 10`. Then `c(k, x)` will not call `c.rv`. To ensure the proper result, wrap the first element in `as.rv`: `c(as.rv(k), x)` will produce a proper random vector.

5 Disclaimer

This program is a work in progress, and it may contain bugs. Many new features will be eventually (and hopefully) added.

For information about random variables in R, please refer to Kerman and Gelman [2007].

References

