Package ‘shrink’

March 9, 2016

Title Global, Parameterwise and Joint Shrinkage Factor Estimation

Version 1.2.1

Description The predictive value of a statistical model can often be improved by applying shrinkage methods. This can be achieved, e.g., by regularized regression or empirical Bayes approaches. Various types of shrinkage factors can also be estimated after a maximum likelihood. While global shrinkage modifies all regression coefficients by the same factor, parameterwise shrinkage factors differ between regression coefficients. With variables which are either highly correlated or associated with regard to contents, such as several columns of a design matrix describing a nonlinear effect, parameterwise shrinkage factors are not interpretable and a compromise between global and parameterwise shrinkage, termed ‘joint shrinkage’, is a useful extension. A computational shortcut to resampling-based shrinkage factor estimation based on DFBETA residuals can be applied. Global, parameterwise and joint shrinkage for models fitted by lm(), glm(), coxph(), or mfp() is available.

Depends R (>= 3.2.2)

License GPL-2

Imports survival, MASS, rms, mfp

LazyData true

Suggests aod, knitr, rmarkdown

VignetteBuilder knitr

RoxygenNote 5.0.1

NeedsCompilation no

Author Daniela Dunkler [aut, cre], Georg Heinze [aut]

Maintainer Daniela Dunkler <daniela.dunkler@meduniwien.ac.at>

Repository CRAN

Date/Publication 2016-03-09 15:21:00
**R topics documented:**

- `shrink-package` .......................................................... 2
- `coef.shrink` .............................................................. 4
- `deepvein` ................................................................. 4
- `GBSG` ....................................................................... 6
- `predict.shrink` ........................................................... 7
- `print.shrink` ............................................................. 8
- `shrink` ..................................................................... 9
- `summary.shrink` .......................................................... 13
- `vcov.shrink` ............................................................. 14

**Index**

`shrink-package` | *Global, Parameterwise and Joint Shrinkage Factor Estimation*

---

**Description**

The predictive value of a statistical model can often be improved by applying shrinkage methods. This can be achieved, e.g., by regularized regression or empirical Bayes approaches. Various types of shrinkage factors can also be estimated after a maximum likelihood. While global shrinkage modifies all regression coefficients by the same factor, parameterwise shrinkage factors differ between regression coefficients. With variables which are either highly correlated or associated with regard to contents, such as several columns of a design matrix describing a nonlinear effect or two main effects and their pairwise interaction term, parameterwise shrinkage factors are not interpretable and a compromise between global and parameterwise shrinkage, termed 'joint shrinkage', is a useful extension. A computational shortcut to resampling-based shrinkage factor estimation based on DFBETA residuals can be applied. Global, parameterwise and joint shrinkage for models fitted by `lm`, `glm`, `coxph`, and `mfp` is available.

**Details**

- **Package:** `shrink`
- **Type:** Package
- **Version:** 1.2.1
- **Date:** 2016-03-09
- **License:** GPL-2

Functions included in the `shrink-package`:

- `shrink` a function to compute global, parameterwise and joint post-estimation shrinkage factors of fit objects of class `lm`, `glm`, `coxph`, or `mfp`.
- `coef.shrink` returns shrunk regression coefficients from objects of class `shrink`.
- `predict.shrink` obtains predictions from shrunked regression coefficients from objects...
shrink-package

of class shrink.

vcov.shrink returns the variance-covariance matrix of shrinkage factors.

print.shrink prints objects of class shrink.

summary.shrink summary of objects of class shrink.

Data set included in the shrink-package:

   deepvein  deep vein thrombosis study
   GBSG     German breast cancer study

References


See Also

*shrink, coef.shrink, predict.shrink, print.shrink, summary.shrink, vcov.shrink, deepvein*

Examples

```r
# with glm, family = binomial
set.seed(888)
intercept <- 1
beta <- c(0.5, 1.2)
n <- 200
x1 <- rnorm(n, mean = 1, sd = 1)
x2 <- rbinom(n, size = 1, prob = 0.3)
prob <- exp(linpred) / (1 + exp(linpred))
rulis <- runif(n, min = 0, max = 1)
ytest <- ifelse(rulis < prob, yes = 1, no = 0)
simdat <- data.frame(cbind(y = ifelse(rulis < prob, 1, 0), x1, x2))

fit <- glm(y ~ x1 + x2, family = binomial, data = simdat, x = TRUE)
summary(fit)

global <- shrink(fit, type = "global", method = "dfbeta")
print(global)
coef(global)

shrink(fit, type = "parameterwise", method = "dfbeta")

shrink(fit, type = "parameterwise", method = "dfbeta", join = list(c("x1", "x2")))
```
# shrink(fit, type = "global", method = "jackknife")
# shrink(fit, type = "parameterwise", method = "jackknife")
# shrink(fit, type = "parameterwise", method = "jackknife",
#        join = list(c("x1", "x2")))

# For more examples see shrink

def description:
    This class of objects is returned by the shrink function. Objects of this class have methods for the functions coef, predict, print, summary, and vcov.

Usage
    ## S3 method for class 'shrink'
    coef(object, ...)

Arguments
    object an object of class shrink.
    ... further arguments.

Value
    A vector with shrunken regression coefficients

See Also
    shrink, print.shrink, predict.shrink, summary.shrink, vcov.shrink

depvein

Description
    A data frame containing time to recurrence of thrombosis and several potential prognostic factors measured at baseline for 929 individuals with deep vein thrombosis or unprovoked pulmonary embolism. 147 events of recurrence were observed during a median follow-up time of 37.8 months.
Usage

deepleein

Format

The data frame contains observations of 929 individuals and the following variables:

- **pnr**  patient number.
- **time**  time to recurrence of thrombosis or end of study in months.
- **status**  = 1 recurrence of thrombosis.
- **sex**  gender.
- **fiimut**  factor II G20210A mutation.
- **fvleid**  factor V Leiden mutation.
- **log2ddim**  log2-transformed D-dimer.
- **bmi**  body mass index.
- **durther**  duration of anticoagulation therapy.
- **age**  age in years.
- **loc**  location of first thrombosis: pulmonary embolism (PE), distal, or proximal deep vein thrombosis.

Note

The data are a modified and partly simulated version of the data set used by Eichinger et al. (2010) and are available under a GPL-2 license.

References


Examples

data("deepvein")
summary(deepvein)
Description

A data frame containing the observations from the GBSG study.

Usage

GBSG

Format

This data frame contains the observations of 686 women:

- **id**: patient id.
- **htreat**: hormonal therapy, a factor at two levels 0 (no) and 1 (yes).
- **age**: age of the patients in years.
- **menostat**: menopausal status, a factor at two levels 1 (premenopausal) and 2 (postmenopausal).
- **tumsize**: tumor size (in mm).
- **tumgrad**: tumor grade, a ordered factor at levels 1 < 2 < 3.
- **posnodal**: number of positive nodes.
- **prm**: progesterone receptor (in fmol).
- **esm**: estrogen receptor (in fmol).
- **rfst**: recurrence free survival time (in days).
- **cens**: censoring indicator (0 censored, 1 event).

References


Examples

data("GBSG")
summary(GBSG)
predict.shrink Predict Method for Objects of Class shrink

Description
Obtains predictions from shrunken regression coefficients from an object of class shrink. This class of objects is returned by the shrink function. Objects of this class have methods for the functions coef, predict, print, summary, and vcov.

Usage
```r
## S3 method for class 'shrink'
predict(object, newdata = NULL, type = c("link", "response", "lp", "risk", "expected", "terms"), shrinktype = NULL, terms = NULL, na.action = na.pass, collapse, safe = FALSE, ...)
```

Arguments
- **object**: an object of class shrink.
- **newdata**: a data frame for which predictions are obtained, otherwise predictions are based on the data stored in object.
- **type**: the type of prediction required.
- **shrinktype**: the type of shrinkage requested, if the object was obtained with type = "all", either "parameterwise" or "global".
- **terms**: with type = "terms" by default all terms are returned. A character vector specifies which terms are to be returned.
- **na.action**: function determining what should be done with missing values in newdata. The default is to include all observations.
- **collapse**: if family = coxph or Cox, an optional vector of subject identifiers. If specified, the output will contain one entry per subject rather than one entry per observation.
- **safe**: option from predict.mfp.
- **...**: additional arguments to be passed to methods.

Value
A vector or matrix of predictions.

Note
If object was obtained using type = "all", shrinktype specifies for which type of shrinkage predictions are requested. shrinktype will be ignored if object was obtained using either type = "parameterwise" or type = "global".
See Also

shrink, coef.shrink, print.shrink, summary.shrink, vcov.shrink

Examples

data("GBSG")
library("mfp")

fit <- mfp(Surv(rfst, cens) ~ fp(age, df = 4, select = 0.05) +
fp(prm, df = 4, select = 0.05), family = cox, data = GBSG)

dfbeta.global <- shrink(fit, type = "global", method = "dfbeta")
dfbeta.pw <- shrink(fit, type = "parameterwise", method = "dfbeta")
dfbeta.join <- shrink(fit, type = "parameterwise", method = "dfbeta",
join=list(c("age.1", "age.2")))

age <- 30:80
newdat <- data.frame(age = age, prm = 0)
refdat <- data.frame(age = 50, prm = 0)

# unshrunken
plot(age, predict(fit, newdata = newdat, type = "lp") -
predict(fit, newdata = refdat, type = "lp"), xlab = "Age",
ylab = "Log hazard relative to 50 years", type = "l", lwd = 2)

# globally shrunken
lines(age, predict(dfbeta.global,newdata = newdat, type = "lp") -
predict(dfbeta.global, newdata = refdat, type = "lp"), lty = 3, col = "red", lwd = 2)

# jointly shrunken
lines(age, predict(dfbeta.join, newdata = newdat, type = "lp") -
predict(dfbeta.join, newdata = refdat, type = "lp"), lty = 4, col = "blue", lwd = 2)

# parameterwise shrunken
lines(age, predict(dfbeta.pw, newdata = newdat, type = "lp") -
predict(dfbeta.pw, newdata =refdat, type = "lp"), lty = 2, col = "green", lwd = 2)

legend("topright", lty = c(1, 3, 4, 2), title = "SHRINKAGE",
legend = c("No", "Global", "Joint", "Parameterwise"), inset = 0.01, bty = "n",
col = c("black", "red", "blue", "green"), lwd = 2)

---

print.shrink

Print Method for Objects of Class shrink

Description

This class of objects is returned by the shrink function. Objects of this class have methods for the functions coef, predict, print, summary, and vcov.
Global, Parameterwise and Joint Shrinkage of Regression Coefficients

Obtain global, parameterwise and joint post-estimation shrinkage factors for regression coefficients from fit objects of class `lm`, `glm`, `coxph`, or `mfp`.

**Usage**

```r
shrink(fit, type = c("parameterwise", "global", "all"),
       method = c("jackknife", "dfbeta"), join = NULL, notes = TRUE,
       postfit = TRUE)
```

**Arguments**

- `fit` a fit object of class `lm`, `glm`, `coxph`, or `mfp`. The fit object must have been called with `x = TRUE` (and `y = TRUE` in case of class `lm`).
- `type` of shrinkage, either "parameterwise" (default), "global" shrinkage, or "all".
- `method` of shrinkage estimation, either "jackknife" (based on leave-one-out resampling, default) or "dfbeta" (excellent approximation based on DFBETA residuals).
- `join` compute optional joint shrinkage factors for sets of specified columns of the design matrix, if `type = "parameterwise"`. See details.
- `notes` print notes. Default is TRUE.
- `postfit` obtain fit with shrunken regression coefficients. This option is only available for models without an intercept. Default is TRUE.
Details

While global shrinkage modifies all regression coefficients by the same factor, parameterwise shrinkage factors differ between regression coefficients. With variables which are either highly correlated or associated with regard to contents, such as several columns of a design matrix describing a nonlinear effect, parameterwise shrinkage factors are not interpretable. Joint shrinkage of a set of such associated design variables will give one common shrinkage factor for this set.

Joint shrinkage factors may be useful when analysing highly correlated and/or such associated columns of the design matrix, e.g. dummy variables corresponding to a categorical explanatory variable with more than two levels, two variables and their pairwise interaction term, or several transformations of an explanatory variable enabling estimation of nonlinear effects. The analyst can define 'joint' shrinkage factors by specifying the join option if type = "parameterwise". join expects a list with at least one character vector including the names of the columns of the design matrix for which a joint shrinkage factor is requested. For example the following specification of join = list(c("dummy1", "dummy2", "dummy3"), c("main1", "main2", "interaction"), c("varX.fp1", "varX.fp2")) requests the joint shrinkage factors for a) "dummy1", "dummy2" and "dummy3", b) "main1", "main2" and "interaction" and c) "varX.fp1" and "varX.fp2".

Restricted cubic splines using rcs: shrink also works for models incorporating restricted cubic splines computed with the rcs function from the rms package. A joint shrinkage factor of explanatory variable varX transformed with rcs can be obtained by join = list(c("rcs(varX)")) or by stating the names of the rcs-transformed variables as given in the respective fit object. (These two notations should not be mixed within one call to shrink.)

Jackknife versus DFBETA method: For linear regression models (lm or glm with family = "gaussian") shrinkage factors obtained by Jackknife and the DFBETA approximation will be identical. For all other types of regression, the computational effort of estimating shrinkage factors may be greatly reduced by using method = "dfbeta" instead. However, for (very) small data sets method = "jackknife" may be of advantage, as the use of DFBETA residuals may underestimate the influence of some highly influential observations.

Shrunken intercept: A shrunken intercept is estimated as follows: For all columns of the design matrix except for the intercept the shrinkage factors are multiplied with the respective regression coefficients and a linear predictor is computed. Then the shrunken intercept is estimated by modeling fit$y ~ offset(linear predictor). For regression models without an intercept, i.e., fit objects of class coxph, the shrunken regression coefficients can be directly estimated. This postfit is retained in the $postfit component of the shrink object.

Value

shrink returns an object with the following components:

- ShrinkageFactors: a vector of shrinkage factors of regression coefficients.
- ShrinkageFactorsVCOV: the covariance matrix of the shrinkage factors.
- ShrunkenRegCoef: a vector with the shrunken regression coefficients.
- postfit: an optional postfit model with shrunken regression coefficients and associated standard errors for models without an intercept.
- fit: the original (unshrunken) fit object.
- type: the requested shrinkage type.
shrink

method the requested shrinkage method.
join the requested joint shrinkage factors.
call the function call.

If type = "all" then the object returned by shrink additionally contains

global a list with the following elements: ShrinkageFactors, ShrinkageFactorsVCOV and ShrunkenRegCoef.
parameterwise a list with the following elements: ShrinkageFactors, ShrinkageFactorsVCOV and ShrunkenRegCoef.
joint an optional list with the following elements: ShrinkageFactors, ShrinkageFactorsVCOV and ShrunkenRegCoef.

Note

For fit objects of class mfp with family != cox regression coefficients of fit (obtained by coef(fit)) and fit$fit may not always be identical, because of mfp's pretransformation applied to the explanatory variables in the model. The shrink function uses a) the names as given in names(coef(fit)) and b) the regression coefficients as given in summary(fit) which correspond to the pretransformed explanatory variables.

References


See Also

coef.shrink, predict.shrink, print.shrink, summary.shrink, vcov.shrink

Examples

## Example with mfp (family = cox)
data("GBSG")
library("mfp")
fit1 <- mfp(Surv(rfst, cens) ~ fp(age, df = 4, select = 0.05) +
fp(prm, df = 4, select = 0.05), family = cox, data = GBSG)

shrink(fit1, type = "global", method = "dfbeta")

dfbeta.pw <- shrink(fit1, type = "parameterwise", method = "dfbeta")
dfbeta.pw
dfbeta.pw$postfit

# correlations between shrinkage factors and standard errors of shrinkage factors
cov2cor(dfbeta.pw$ShrinkageFactorsVCOV)
sqrt(diag(dfbeta.pw$ShrinkageFactorsVCOV))

shrink(fit1, type = "parameterwise", method = "dfbeta",
       join = list(c("age.1", "age.2")))

# shrink(fit1, type = "global", method = "jackknife")
# shrink(fit1, type = "parameterwise", method = "jackknife")
# shrink(fit1, type = "parameterwise", method = "jackknife",
#        join = list(c("age.1", "age.2")))

# obtain global, parameterwise and joint shrinkage with one call to 'shrink'
shrink(fit1, type = "all", method = "dfbeta",
        join = list(c("age.1", "age.2")))

## Example with rcs
library("rms")
fit2 <- coxph(Surv(rfst, cens) ~ rcs(age) + log(prm + 1), data = GBSG, x = TRUE)

shrink(fit2, type = "global", method = "dfbeta")
shrink(fit2, type = "parameterwise", method = "dfbeta")
shrink(fit2, type = "parameterwise", method = "dfbeta",
        join = list(c("rcs(age)")))
shrink(fit2, type = "parameterwise", method = "dfbeta",
        join = list(c("rcs(age)"), c("log(prm + 1)")))

## Examples with glm & mfp (family = binomial)
set.seed(888)
intercept <- 1
beta <- c(0.5, 1.2)
n <- 1000
x1 <- rnorm(n, mean = 1, sd = 1)
x2 <- rbinom(n, size = 1, prob = 0.3)
prob <- exp(linpred) / (1 + exp(linpred))
runis <- runif(n, 0, 1)
ytest <- ifelse(runis < prob, yes = 1, no = 0)
simdat <- data.frame(cbind(y = ifelse(runis < prob, 1, 0), x1, x2))

fit3 <- glm(y ~ x1 + x2, family = binomial, data = simdat, x = TRUE)
summary(fit3)

shrink(fit3, type = "global", method = "dfbeta")
shrink(fit3, type = "parameterwise", method = "dfbeta")
shrink(fit3, type = "parameterwise", method = "dfbeta",
        join = list(c("x1", "x2")))

utils::data("Pima.te", package="MASS")
utils::data("Pima.tr", package="MASS")
Pima <- rbind(Pima.te, Pima.tr)
fit4 <- mfp(type = npreg + glu + bmi + ped + fp(age, select = 0.05),
            family = binomial, data = Pima)
summary(fit4)
shrink(fit4, type = "global", method = "dfbeta")
shrink(fit4, type = "parameterwise", method = "dfbeta")
# fit objects of class mfp: for 'join' use variable names as given in 'names(coef(fit4))'
shrink(fit4, type = "parameterwise", method = "dfbeta", join = list(c("age.1")))

## Examples with glm & mfp (family = gaussian) and lm
utils::data("anorexia", package = "MASS")
contrasts(anorexia$Treat) <- contr.treatment(n = 3, base = 2)
fit5 <- glm(Postwt ~ Prewt + Treat, family = gaussian, data = anorexia, x = TRUE)
fit5

shrink(fit5, type = "global", method = "dfbeta")
# which is identical to the more time-consuming jackknife approach:
# shrink(fit5, type = "global", method = "jackknife")
shrink(fit5, type = "parameterwise", method = "dfbeta")
shrink(fit5, type = "parameterwise", method = "dfbeta",
   join = list(c("Treat1", "Treat3")))

fit6 <- lm(Postwt ~ Prewt + Treat, data = anorexia, x = TRUE, y = TRUE)
fit6

shrink(fit6, type = "global", method = "dfbeta")
shrink(fit6, type = "parameterwise", method = "dfbeta")
shrink(fit6, type = "parameterwise", method = "dfbeta",
   join=list(c("Treat1", "Treat3")))

utils::data("GAGurine", package = "MASS")
fit7 <- mfp(Age ~ fp(GAG, select = 0.05), family = gaussian, data = GAGurine)
summary(fit7)

shrink(fit7, type = "global", method = "dfbeta")
shrink(fit7, type = "parameterwise", method = "dfbeta")
# fit objects of class mfp: for 'join' use variable names as given in 'names(coef(fit7))'
shrink(fit7, type = "parameterwise", method = "dfbeta",
   join = list(c("GAG.1", "GAG.2")))

summary.shrink

## Summary Method for Objects of Class shrink

**Description**

This class of objects is returned by the shrink function. Objects of this class have methods for the functions coef, predict, print, summary, and vcov.
Usage

```r
## S3 method for class 'shrink'
summary(object, digits = 6, ...)
```

Arguments

- `object`: an object of class `shrink`.
- `digits`: integer, used for number formatting with `signif()`.
- `...`: further arguments.

Value

A matrix with regression coefficients of the original fit, corresponding shrinkage factors and shrunken regression coefficients.

See Also

`shrink`, `coef.shrink`, `print.shrink`, `predict.shrink`, `vcov.shrink`

---

**vcov.shrink**

Calculate Variance-Covariance Matrix of Shrinkage Factors for Objects of Class `shrink`

---

Description

This class of objects is returned by the `shrink` function. Objects of this class have methods for the functions `coef`, `predict`, `print`, `summary`, and `vcov`.

Usage

```r
## S3 method for class 'shrink'
vcov(object, digits = 6, ...)
```

Arguments

- `object`: object of class `shrink`.
- `digits`: integer, used for number formatting with `signif()`.
- `...`: further arguments.

Value

A matrix of the estimated covariances between the obtained shrinkage factors.

See Also

`shrink`, `coef.shrink`, `predict.shrink`, `print.shrink`, `summary.shrink`
Index

*Topics datasets
  - deepvein, 4
  - GBSG, 6

coeff.shrink, 3, 4, 8, 9, 11, 14

deepervein, 3, 4

GBSG, 6

predict.shrink, 3, 4, 7, 9, 11, 14

print.shrink, 3, 4, 8, 9, 11, 14

rcs, 10

shrink, 3, 4, 8, 9, 9, 14

shrink-package, 2

signif, 14

summary.shrink, 3, 4, 8, 9, 11, 13, 14

vcov.shrink, 3, 4, 8, 9, 11, 14, 14