Package ‘ucminf’

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Title General-Purpose Unconstrained Non-Linear Optimization
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Description An algorithm for general-purpose unconstrained non-linear optimization. The algorithm is of quasi-Newton type with BFGS updating of the inverse Hessian and soft line search with a trust region type monitoring of the input to the line search algorithm. The interface of 'ucminf' is designed for easy interchange with 'optim'.
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ucminf General-Purpose Unconstrained Non-Linear Optimization

Description

An algorithm for general-purpose unconstrained non-linear optimization. The algorithm is of quasi-Newton type with BFGS updating of the inverse Hessian and soft line search with a trust region type monitoring of the input to the line search algorithm. The interface of ‘ucminf’ is designed for easy interchange with ‘optim’.

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Usage

ucminf(par, fn, gr = NULL, ..., control = list(), hessian=0)

Arguments

par Initial estimate of minimum for fn.
fn Objective function to be minimized.
gr Gradient of objective function. If NULL a finite difference approximation is used.
... Optional arguments passed to the objective and gradient functions.
control A list of control parameters. See ‘Details’.
hessian Integer value:
   0 No hessian approximation is returned.
   1 Returns a numerical approximation of the Hessian using ‘hessian’ in the package ‘numDeriv’.
   2 Returns final approximation of the inverse Hessian based on the series of BFGS updates during optimization.
   3 Same at 2, but will also return the Hessian (the inverse of 2).

If a TRUE or FALSE value is given it will switch between option 1 or 0.

Details

The algorithm is documented in (Nielsen, 2000) (see References below) together with a comparison to the Fortran subroutine ‘MINF’ and the Matlab function ‘fminunc’. The implementation of ‘ucminf’ in R uses the original Fortran version of the algorithm.

The interface in R is designed so that it is very easy to switch between using ‘ucminf’ and ‘optim’. The arguments par, fn, gr, and hessian are all the same (with a few extra options for hessian in ‘ucminf’). The difference is that there is no method argument in ‘ucminf’ and that some of the components in the control argument are different due to differences in the algorithms.

The algorithm can be given an initial estimate of the Hessian for the optimization and it is possible to get the final approximation of the Hessian based on the series of BFGS updates. This extra functionality may be useful for optimization in a series of related problems.

The functions fn and gr can return Inf or NaN if the functions cannot be evaluated at the supplied value, but the functions must be computable at the initial value. The functions are not allowed to return NA. Any names given to par will be copied to the vectors passed to fn and gr. No other attributes of par are copied over.

The control argument is a list that can supply any of the following components:

trace If trace is positive then detailed tracing information is printed for each iteration.
grtol The algorithm stops when \[ \|F'(x)\|_\infty \leq \text{grtol} \], that is when the largest absolute value of the gradient is less than grtol. Default value is grtol = 1e-6.
xtol The algorithm stops when \[ \|x - x_p\|_2 \leq xtol \cdot (xtol + \|x\|_2), \] where \( x_p \) and \( x \) are the previous and current estimate of the minimizer. Thus the algorithm stops when the last relative step length is sufficiently small. Default value is xtol = 1e-12.
**ucminf**

**stepmax** Initial maximal allowed step length (radius of trust-region). The value is updated during the optimization. Default value is `stepmax = 1`.

**maxeval** The maximum number of function evaluations. A function evaluation is counted as one evaluation of the objective function and of the gradient function. Default value is `maxeval = 500`.

**grad** Either ‘forward’ or ‘central’. Controls the type of finite difference approximation to be used for the gradient if no gradient function is given in the input argument ‘gr’. Default value is `grad = ‘forward’`.

**gradstep** Vector of length 2. The step length in finite difference approximation for the gradient. Step length is `|x| \cdot gradstep[1]+gradstep[2]`. Default value is `gradstep = c(1e-6, 1e-8)`.

**invhessian.lt** A vector with an initial approximation to the lower triangle of the inverse Hessian. If not given, the inverse Hessian is initialized as the identity matrix. If $H_0$ is the initial hessian matrix then the lower triangle of the inverse of $H_0$ can be found as `invhessian.lt = solve(H0)[lower.tri(H0, diag=0)]`.

**Value**

- **par** Computed minimizer.
- **value** Objective function value at computed minimizer.
- **convergence** Flag for reason of termination:
  - 1 Stopped by small gradient (grtol).
  - 2 Stopped by small step (xtol).
  - 3 Stopped by function evaluation limit (maxeval).
  - 4 Stopped by zero step from line search
  - -2 Computation did not start: length(par) = 0.
  - -4 Computation did not start: stepmax is too small.
  - -5 Computation did not start: grtol or xtol <= 0.
  - -6 Computation did not start: maxeval <= 0.
  - -7 Computation did not start: given Hessian not pos. definite.
- **message** String with reason of termination.
- **hessian, invhessian**
  - Estimate of (inv.) Hessian at computed minimizer. The type of estimate is given by the input argument ‘hessian’.
  - **invhessian.lt** The lower triangle of the final approximation to the inverse Hessian based on the series of BFGS updates during optimization.
- **info** Information about the search:
  - **maxgradient** $||F'(x)||_\infty$, the largest element in the absolute value of the gradient at the computed minimizer.
  - **laststep** Length of last step.
  - **stepmax** Final maximal allowed step length.
  - **neval** Number of calls to both objective and gradient function.
Author(s)

‘UCMINF’ algorithm design and Fortran code by Hans Bruun Nielsen.
Implementation in R by Stig B. Mortensen, <stigbm@gmail.com>.
Modifications by Douglas Bates <bates@stat.wisc.edu>, Nov. 2010, to support nested optimization
and correct issues with printing on Windows.

References

Report IMM-REP-2000-18, Department of Mathematical Modelling, Technical University of Den-
The original Fortran source code can be found at http://www2.imm.dtu.dk/projects/hbn_software/
ucminf.f. The code has been slightly modified in this package to be suitable for use with R.
The general structure of the implementation in R is based on the package ‘FortranCallsR’ by Di-
ethelm Wuertz.

See Also

optim, nlminb, nlm.

Examples

## Rosenbrock Banana function
fr <- function(x) (1 - x[1])^2 + 100 * (x[2] - x[1]^2)^2
gR <- function(x) c(-400 * x[1] * (x[2] - x[1] * x[1]) - 2 * (1 - x[1]),

# Find minimum and show trace
ucminf(par = c(2,.5), fn = fr, gr = gR, control = list(trace = 1))
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