Package ‘neldermead’

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Title R Port of the 'Scilab' Neldermead Module
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Suggests knitr (>= 1.28),rmarkdown (>= 2.2)
Description Provides several direct search optimization algorithms based on the simplex method. The provided algorithms are direct search algorithms, i.e. algorithms which do not use the derivative of the cost function. They are based on the update of a simplex. The following algorithms are available: the fixed shape simplex method of Spendley, Hext and Himsworth (unconstrained optimization with a fixed shape simplex, 1962) <doi:10.1080/00401706.1962.10490033>, the variable shape simplex method of Nelder and Mead (unconstrained optimization with a variable shape simplex made, 1965) <doi:10.1093/comjnl/7.4.308>, and Box's complex method (constrained optimization with a variable shape simplex, 1965) <doi:10.1093/comjnl/8.1.42>.
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R topics documented:

  neldermead-package ................................................. 2
  costf.transpose .................................................. 5
The goal of this package is to provide a Nelder-Mead direct search optimization method. That Nelder-Mead algorithm may be used in the following optimization context:

- there is no need to provide the derivatives of the objective function,
- the number of parameters is small (up to 10-20),
- there are bounds and/or non linear constraints.

Design

This package provides the following components:

- **neldermead** provides various Nelder-Mead variants and manages for Nelder-Mead specific settings, such as the method to compute the initial simplex, the specific termination criteria,
- **fminsearch** provides a simplified Nelder-Mead algorithm. Specific termination criteria, initial simplex and auxiliary settings are automatically configured.
- **fminbnd** provides a simplified Box algorithm, i.e. the equivalent of **fminsearch** for unconstrained search.
- **optimset**, **optimget** provide commands to emulate their Scilab counterparts.
- **optimplotfunccount**, **optimplotx** and **optimplotfval** provide plotting features for the **fminsearch** function (Not implemented yet).
• `nmplot` provides a high-level component which provides directly output pictures for Nelder-Mead algorithm. (Not implemented yet).

The current component is based on the following packages

• **optimbase**: provides an abstract class for a general optimization component, including the number of variables, the minimum and maximum bounds, the number of non linear inequality constraints, the loggin system, various termination criteria, the cost function, etc...

• **optimsimplex**: provides a class to manage a simplex made of an arbitrary number of vertices, including the computation of a simplex by various methods (axes, regular, Pfeffer’s, randomized bounds), the computation of the size by various methods (diameter, sigma+, sigma-, etc...)

**Features**

The following is a list of features the Nelder-Mead prototype algorithm currently provides:

• Provides 3 algorithms, including
  – the fixed shape algorithm of Spendley et al.,
  – the variable shape algorithm of Nelder and Mead,
  – Box’s ‘complex’ algorithm managing bounds and nonlinear inequality constraints based on arbitrary number of vertices in the simplex.

• Manage various simplex initializations:
  – initial simplex given by user,
  – initial simplex computed with a length and along the coordinate axes,
  – initial regular simplex computed with formula of Spendley et al.,
  – initial simplex computed by a small perturbation around the initial guess point.

• Manage cost function:
  – optional additional argument,
  – direct communication of the task to perform: cost function or inequality constraints.

• Manage various termination criteria, including maximum number of iterations, tolerance on function value (relative or absolute):
  – tolerance on x (relative or absolute),
  – tolerance on standard deviation of function value (original termination criteria in Box 1965),
  – maximum number of evaluations of cost function,
  – absolute or relative simplex size.

• Manage the history of the convergence, including:
  – history of function values,
  – history of optimum point,
  – history of simplices,
  – history of termination criteria.

• Provide a plot command which allows to graphically see the history of the simplices toward the optimum (Not yet implemented).
• Provide query features for the status of the optimization process: number of iterations, number of function evaluations, status of execution, function value at initial point, function value at optimal point, etc...
• Kelley restart based on simplex gradient.
• O’Neill restart based on factorial search around optimum.

Details

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<th>neldermead</th>
</tr>
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<tbody>
<tr>
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<td>Package</td>
</tr>
<tr>
<td>Version</td>
<td>1.0-12</td>
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See vignette('neldermead',package='neldermead') for more information.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References

'Detection and Remediation of Stagnation in the Nelder–Mead Algorithm Using a Sufficient Decrease Condition', Kelley C. T., SIAM J. on Optimization, 1999

See Also

optimbase optimsimplex
Description

Call the cost function after transposition of the value of the point estimate x, so that the input row vector, given by optim simplex, is transposed into a column vector as required by the cost function.

Usage

costf.transposex(x = NULL, this = NULL)

Arguments

x

The point estimate provide as a row matrix.

this

A neldermead object.

Value

Return the value of the cost function (called by neldermead.costf.)

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

neldermead.costf

fmin.gridsearch

Grid evaluation of an unconstrained cost function

Description

Evaluate an unconstrained cost function on a grid of points around a given initial point estimate.

Usage

fmin.gridsearch(fun = NULL, x0 = NULL, xmin = NULL, xmax = NULL, npts = 3, alpha = 10)
Arguments

fun
An unconstrained cost function returning a numeric scalar, similar to those used in the fminsearch function.

x0
The initial point estimate, provided as a numeric vector.

xmin
Optional: a vector of lower bounds.

xmax
Optional: a vector of upper bounds.

npts
An integer scalar greater than 2, indicating the number of evaluation points will be used on each dimension to build the search grid.

alpha
A vector of numbers greater than 1, which give the factor(s) used to calculate the evaluation range of each dimension of the search grid (see Details). If alpha length is lower than that of x0, elements of alpha are recycled. If its length is higher than that of x0, alpha is truncated.

Details

fmin.gridsearch evaluates the cost function at each point of a grid of npts\cdot length(x0) points. If lower (xmin) and upper (xmax) bounds are provided, the range of evaluation points is limited by those bounds and alpha is not used. Otherwise, the range of evaluation points is defined as \[x0/alpha,x0*alpha\].

The actual evaluation of the cost function is delegated to optimbase.gridsearch.

Value

Return a data.frame with the coordinates of the evaluation point, the value of the cost function and its feasibility. Because the cost function is unconstrained, it is always feasible. The data.frame is ordered by feasibility and increasing value of the cost function.

Author(s)

Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

fminsearch, optimbase.gridsearch

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fminbnd

*Computation of the constrained minimum of given function with the Nelder-Mead algorithm.*
Description

EXPERIMENTAL.

This function searches for the constrained minimum of a given cost function. The provided algorithm is a direct search algorithm, i.e. an algorithm which does not use the derivative of the cost function. It is based on the update of a simplex, which is a set of \( k \geq n+1 \) vertices, where each vertex is associated with one point, which coordinates are constrained within user-defined boundaries, and with one function value. This algorithm corresponds to a version of the Box algorithm, based on bounds and no non-linear constraints. This function is based on a specialized use of the more general neldermead function bundle. Users who want to have a more flexible solution based on direct search algorithms should consider using the neldermead functions instead of the fminbnd function.

Usage

\[
fminbnd(fun=NULL, x0=NULL, xmin=NULL, xmax=NULL, options=NULL, verbose=FALSE)
\]

Arguments

- **fun**: A cost function return a numeric scalar.
- **x0**: A numerical vector of initial guesses (length \( n \)).
- **xmin**: A numerical vector of lower bounds for \( x0 \) (length \( n \)).
- **xmax**: A numerical vector of upper bounds for \( x0 \) (length \( n \)).
- **options**: A list of optimization options, which drives the behaviour of fminbnd. These options must be set with the optimset function (see ?optimset) which returns a list with the following elements:
  - **MaxIter**: The maximum number of iterations. The default is 200 * \( n \).
  - **MaxFunEvals**: The maximum number of evaluations of the cost function. The default is 200 * \( n \).
  - **BoxTolFun**: The absolute tolerance on function value. The default value is 1.e-4.
  - **TolFun**: The absolute tolerance on function value. The default value is 1.e-4.
  - **TolX**: The absolute tolerance on simplex size. The default value is 1.e-4.
  - **Display**: The verbose level.
  - **OutputFcn**: The output function, or a list of output functions called at the end of each iteration. The default value is NULL.
  - **PlotFcns**: The plot function, or a list of plotfunction functions called at the end of each iteration. The default value is empty.
- **verbose**: The verbose option, controlling the amount of messages.

Details

Termination criteria

In this section, we describe the termination criteria used by fminbnd. The criteria is based on the following variables:

- **boxkount**: the current number of time the tolerance on the cost function was met, and
The fminbnd algorithm uses a special initial simplex, which is an heuristic depending on the initial guess. The strategy chosen by fminbnd corresponds to the content of simplex0method element of the neldermead object (set to 'randbounds'). It is applied using the content of the boundsmin and boundsmax elements to generate a simplex with random vertices within the boundaries defined by the user (i.e., xmin, and xmax). This method is an heuristic which is presented in 'A New Method of Constrained Optimization and a Comparison With Other Methods' by M.J. Box. See in the help of optim simplex for more details.

The number of iterations
In this section, we present the default values for the number of iterations in fminbnd.

The options input argument is an optional list which can contain the MaxIter field, which stores the maximum number of iterations. The default value is 200n, where n is the number of variables. The factor 200 has not been chosen by chance, but is the result of experiments performed against quadratic functions with increasing space dimension. This result is presented in 'Effect of dimensionality on the Nelder-Mead simplex method' by Lixing Han and Michael Neumann. This paper is based on Lixing Han’s PhD, ‘Algorithms in Unconstrained Optimization’. The study is based on numerical experiments with a quadratic function where the number of terms depends on the dimension of the space (i.e. the number of variables). Their study showed that the number of iterations required to reach the tolerance criteria is roughly 100n. Most iterations are based on inside contractions. Since each step of the Nelder-Mead algorithm only require one or two function evaluations, the number of required function evaluations in this experiment is also roughly 100n.

Output and plot functions
The optimset function can be used to configure one or more output and plot functions. The output or plot function is expected to have the following definition:

```r
myfun <- function(x, optimValues, state)
```

The input arguments x, optimValues and state are described in detail in the optimset help page. The optimValues$procedure field represents the type of step performed at the current iteration and can be equal to one of the following strings:

- " (the empty string),
- 'initial simplex',
- 'reflect (Box)'.

Value
Return a object of class neldermead. Use the neldermead.get to extract the following element from the returned object:

- **xopt** The vector of n numeric values, minimizing the cost function.
- **fopt** The minimum value of the cost function.
- **exitflag** The flag associated with exist status of the algorithm. The following values are available:
- 1 The maximum number of iterations has been reached.
0  The maximum number of function evaluations has been reached.
1  The tolerance on the simplex size and function value delta has been reached. This signifies
    that the algorithm has converged, probably to a solution of the problem.

output  A list which stores detailed information about the exit of the algorithm. This list contains
         the following fields:
        
        algorithm  A string containing the definition of the algorithm used, i.e. 'Nelder-Mead simplex
direct search'.
        funcCount  The number of function evaluations.
        iterations  The number of iterations.
        message  A string containing a termination message.

Author(s)

Author: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

optimset

Examples

# In the following example, we use the fminbnd function to compute the minimum
# of a quadratic function. We first define the function 'quad', and then use
# the fminbnd function to search the minimum, starting with the initial guess
# (1.2, 1.9) and bounds of (1, 1) and (2, 2). In this particular case, 11
# iterations are performed with 20 function evaluations
quad <- function(x){
    y <- x[1]^2 + x[2]^2
}
sol <- fminbnd(quad,c(1.2,1.9),c(1,1),c(2,2))
summary(sol)

fminbnd.function  fminbnd Cost Function Call

Description

This function calls the cost function and makes it match neldermead requirements. It is used in
the fminbnd function as the function element of the neldermead object (see ?neldermead and
?neldermead.set).

Usage

fminbnd.function(x = NULL, index = NULL, fmsfundata = NULL)
Arguments

- **x**: A single column vector of parameter estimates.
- **index**: An integer variable set to 2, indicating that only the cost function is to be computed by the algorithm.
- **fmsfndata**: An object of class 'optimbase.functionargs' and with (at least) a \*fun\* element, which contains the user-defined cost function.

Value

Returns a list with the following elements:

- **f**: The value of the cost function at the current point estimate.
- **index**: The same index variable.
- **this**: A list with a single element \*costargument\* which contains \*fmsfndata\*.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

- fminbnd, neldermead, neldermead.set

Description

This function calls the output function and make it match neldermead requirements. It is used in the fminbnd function as the outputcommand element of the neldermead object (see ?neldermead and ?neldermead.set).

Usage

fminbnd.outputfun(state = NULL, data = NULL, fmsdata = NULL)

Arguments

- **state**: The current state of the algorithm either 'init', 'iter' or 'done'.
- **data**: The data at the current state. This is an object of class 'neldermead.data', i.e. a list with the following elements:
  - **x**: The current parameter estimates.
  - **fval**: The current value of the cost function.
  - **simplex**: The current simplex object.
**fminsearch**

- **iteration** The number of iterations performed.
- **funccount** The number of function evaluations.
- **step** The type of step in the previous iteration.

**fmsdata**

This is an object of class 'optimbase.functionargs' which contains specific data of the fminbnd algorithm:

- **Display** what to display
- **OutputFcn** the array of output functions
- **PlotFcns** the array of plot functions

**Value**

This function does not return any data, but execute the output function(s).

**Author(s)**

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

**See Also**

fminbnd, neldermead, neldermead.set.

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**Description**

This function searches for the unconstrained minimum of a given cost function. The provided algorithm is a direct search algorithm, i.e. an algorithm which does not use the derivative of the cost function. It is based on the update of a simplex, which is a set of k=n+1 vertices, where each vertex is associated with one point and one function value. This algorithm is the Nelder-Mead algorithm. This function is based on a specialized use of the more general neldermead function bundle. Users who want to have a more flexible solution based on direct search algorithms should consider using the neldermead functions instead of the fminsearch function.

**Usage**

fminsearch(fun = NULL, x0 = NULL, options = NULL, verbose=FALSE)
Arguments

- **fun**: A cost function return a numeric scalar.
- **x0**: A numerical vector of initial guesses (length n).
- **options**: A list of optimization options, which drives the behaviour of fminsearch. These options must be set with the optimset function (see ?optimset) which returns a list with the following elements:
  - **MaxIter**: The maximum number of iterations. The default is $200 \times n$.
  - **MaxFunEvals**: The maximum number of evaluations of the cost function. The default is $200 \times n$.
  - **TolFun**: The absolute tolerance on function value. The default value is $1.e-4$.
  - **TolX**: The absolute tolerance on simplex size. The default value is $1.e-4$.
  - **Display**: The verbose level.
  - **OutputFcn**: The output function, or a list of output functions called at the end of each iteration. The default value is NULL.
  - **PlotFcns**: The plot function, or a list of plotput functions called at the end of each iteration. The default value is empty.
- **verbose**: The verbose option, controlling the amount of messages.

Details

**Termination criteria**

In this section, we describe the termination criteria used by fminsearch. The criteria is based on the following variables:

- **ssize**: the current simplex size,
- **shiftfv**: the absolute value of the difference of function value between the highest and lowest vertices.

If both $ssize < \text{options}$TolX and $shiftfv < \text{options}$TolFun conditions are true, then the iterations stop. The size of the simplex is computed using the 'sigmaplus' method of the optimsimplex package. The 'sigmamplus' size is the maximum length of the vector from each vertex to the first vertex. It requires one loop over the vertices of the simplex.

**The initial simplex**

The fminsearch algorithm uses a special initial simplex, which is an heuristic depending on the initial guess. The strategy chosen by fminsearch corresponds to the content of simplex0method element of the neldermead object (set to 'pfeffer'). It is applied using the content of the simplex0deltausual (0.05) and simplex0deltazero (0.0075) elements. Pfeffer's method is an heuristic which is presented in 'Global Optimization Of Lennard-Jones Atomic Clusters' by Ellen Fan. It is due to L. Pfeffer at Stanford. See in the help of optimsimplex for more details.

**The number of iterations**

In this section, we present the default values for the number of iterations in fminsearch.

The options input argument is an optional list which can contain the MaxIter field, which stores the maximum number of iterations. The default value is $200n$, where $n$ is the number of variables. The factor 200 has not been chosen by chance, but is the result of experiments performed against
quadratic functions with increasing space dimension. This result is presented in 'Effect of dimensionality on the Nelder-mead simplex method' by Lixing Han and Michael Neumann. This paper is based on Lixing Han's PhD, 'Algorithms in Unconstrained Optimization'. The study is based on numerical experiments with a quadratic function where the number of terms depends on the dimension of the space (i.e. the number of variables). Their study showed that the number of iterations required to reach the tolerance criteria is roughly 100n. Most iterations are based on inside contractions. Since each step of the Nelder-Mead algorithm only require one or two function evaluations, the number of required function evaluations in this experiment is also roughly 100n.

Output and plot functions

The optimset function can be used to configure one or more output and plot functions. The output or plot function is expected to have the following definition:

```r
myfun <- function(x, optimValues, state)
```

The input arguments `x`, `optimValues` and `state` are described in detail in the optimset help page. The `optimValues$procedure` field represents the type of step performed at the current iteration and can be equal to one of the following strings:

- " (the empty string),
- 'initial simplex',
- 'expand',
- 'reflect',
- 'contract inside',
- 'contract outside'.

Value

Return a object of class neldermead. Use the neldermead.get to extract the following element from the returned object:

- `xopt` The vector of n numeric values, minimizing the cost function.
- `fopt` The minimum value of the cost function.
- `exitflag` The flag associated with exist status of the algorithm. The following values are available:
  - -1 The maximum number of iterations has been reached.
  - 0 The maximum number of function evaluations has been reached.
  - 1 The tolerance on the simplex size and function value delta has been reached. This signifies that the algorithm has converged, probably to a solution of the problem.
- `output` A list which stores detailed information about the exit of the algorithm. This list contains the following fields:
  - `algorithm` A string containing the definition of the algorithm used, i.e. 'Nelder-Mead simplex direct search'.
  - `funcCount` The number of function evaluations.
  - `iterations` The number of iterations.
  - `message` A string containing a termination message.
Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References


See Also

optimset neldermead

Examples

#In the following example, we use the fminsearch function to compute the minimum
#of the Rosenbrock function. We first define the function 'banana', and then use
#the fminsearch function to search the minimum, starting with the initial guess
#(-1.2, 1.0). In this particular case, 85 iterations are performed with 159
#function evaluations

banana <- function(x){
  y <- 100*(x[2]-x[1]^2)^2 + (1-x[1])^2
}
sol <- fminsearch(banana, c(-1.2,1))
sol

#In the following example, we configure the absolute tolerance on the size of
#the simplex to a larger value, so that the algorithm performs less iterations.
#Since the default value of 'TolX' for the fminsearch function is 1.e-4, we
#decide to use 1.e-2. The optimset function is used to create an optimization
#option list and the field 'TolX' is set to 1.e-2. The options list is then
#passed to the fminsearch function as the third input argument. In this
#particular case, the number of iterations is 70 with 130 function evaluations.

opt <- optimset(TolX=1.e-2)
sol <- fminsearch(banana, c(-1.2,1), opt)
#In the following example, we want to produce intermediate outputs of the algorithm. We define the outfun function, which takes the current point \( x \) as input argument. The function plots the current point into the current graphic window with the plot function. We use the 'OutputFcn' feature of the optimset function and set it to the output function. Then the option list is passed to the fminsearch function. At each iteration, the output function is called back, which creates and update a plot. While this example creates a 2D plot, the user may customized the output function so that it writes a message in the console, write some data into a data file, etc... The user can distinguish between the output function (associated with the 'OutputFcn' option) and the plot function (associated with the 'PlotFcns' option). See the optimset for more details on this feature.

```r
outfun <- function(x, optimValues, state){
  plot(x[1],x[2],xlim=c(-1.5,1.5),ylim=c(-1.5,1.5))
  par(new=TRUE)
}
```

```r
opt <- optimset(OutputFcn=outfun)
sol <- fminsearch(banana, c(-1.2,1), opt)
sol
```

#The 'Display' option allows to get some input about the intermediate steps of the algorithm as well as to be warned in case of a convergence problem. In the following example, we present what happens in case of a convergence problem. We set the number of iterations to 10, instead of the default 400 iterations. We know that 85 iterations are required to reach the convergence criteria. Therefore, the convergence criteria is not met and the maximum number of iterations is reached.

```r
opt <- optimset(MaxIter=10)
sol <- fminsearch(banana, c(-1.2,1), opt)
```

#Since the default value of the 'Display' option is 'notify', a message is generated, which warns the user about a possible convergence problem. The previous script produces the following output.

```
Exiting: Maximum number of iterations has been exceeded
- increase MaxIter option.
Current function value: 4.1355598
```

#In the following example, we present how to display intermediate steps used by the algorithm. We simply set the 'Display' option to the 'iter' value. This option allows to see the number of function evaluations, the minimum function value and which type of simplex step is used for the iteration.

```r
opt <- optimset(Display='iter')
sol <- fminsearch(banana, c(-1.2,1), opt)
sol
```
Description
This function calls the cost function and makes it match neldermead requirements. It is used in the \texttt{fminsearch} function as the \texttt{function} element of the neldermead object (see \texttt{?neldermead} and \texttt{?neldermead.set}).

Usage
\begin{verbatim}
fminsearch.function(x = NULL, index = NULL, fmsfundata = NULL)
\end{verbatim}

Arguments
\begin{itemize}
\item \texttt{x} A single column vector of parameter estimates.
\item \texttt{index} An integer variable set to 2, indicating that only the cost function is to be computed by the algorithm.
\item \texttt{fmsfundata} An object of class \texttt{optimbase.functionargs} and with (at least) a \texttt{fun} element, which contains the user-defined cost function.
\end{itemize}

Value
Returns a list with the following elements:
\begin{itemize}
\item \texttt{f} The value of the cost function at the current point estimate.
\item \texttt{index} The same \texttt{index} variable.
\item \texttt{this} A list with a single element \texttt{costargument} which contains \texttt{fmsfundata}.
\end{itemize}

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
\begin{verbatim}
fminsearch, neldermead, neldermead.set.
\end{verbatim}

---

\texttt{fminsearch.outputfun}  \texttt{fminsearch Output Function Call}

Description
This function calls the output function and make it match neldermead requirements. It is used in the \texttt{fminsearch} function as the \texttt{outputcommand} element of the neldermead object (see \texttt{?neldermead} and \texttt{?neldermead.set}).

Usage
\begin{verbatim}
fminsearch.outputfun(state = NULL, data = NULL, fmsdata = NULL)
\end{verbatim}
Arguments

state
The current state of the algorithm either 'init', 'iter' or 'done'.

data
The data at the current state. This is an object of class 'neldermead.data', i.e. a list with the following elements:

x  The current parameter estimates.

fval  The current value of the cost function.

simplex  The current simplex object.

iteration  The number of iterations performed.

funcount  The number of function evaluations.

step  The type of step in the previous iteration.

fmsdata
This is an object of class 'optimbase.functionargs' which contains specific data of the fminsearch algorithm:

Display  what to display

OutputFcn  the array of output functions

PlotFcns  the array of plot functions

Value

This function does not return any data, but execute the output function(s).

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

fminsearch, neldermead, neldermead.set,
neldermead(optimbase, method, simplex0, simplex0method,
  simplex0length, simplex0size0, simplexopt, historiesimplex, coords0, rho, chi,
  gamma, sigma, tolfstdeviation, tolfstdeviationmethod, tolsimplexizeabsolute,
  tolsimplexizerelative, tolsimplexizemethod, toldeltafv, tolssizedeltafvmethod,
  simplex0deltausual, simplex0deltazero, restartsimplexmethod, restartmax,
  restarteps, restartstep, restartflag, restartdetection,
  kelleystagnationflag, kelleynormalizationflag, kelleystagnationalpha0,
  kelleyalpha, startupflag, boxnbpoints, boxnbpointseff, boxineqscaling,
  checkcostfunction, scalingsimplex0, guinalphamin, boxboundsalpha,
  boxtermination, boxtolf, boxnbmatch, boxkount, boxreflect, tolvarianceflag,
  tolabsolutevariance, tolrelativevariance, variancesimplex0, mymethod,
  myterminate, myterminateflag, greedy, output, exitflag)

## S3 method for class 'neldermead'
print(x, verbose, ...)

## S3 method for class 'neldermead'
summary(object, showhistory, ...)

## S3 method for class 'neldermead'
is(x = NULL)

Arguments

optbase
  An object of class 'optimbase', i.e. a list created by optimbase() and containing
  the following elements:
  verbose The verbose option, controlling the amount of messages.
  x0 The initial guess.
  fx0 The value of the function for the initial guess.
  xopt The optimum parameter.
  fopt The optimum function value.
  tolfunabsolute The absolute tolerance on function value.
  tolfunrelative The relative tolerance on function value.
  tolfunmethod Logical flag for the tolerance on function value in the termination
    criteria. This criteria is suitable for functions which minimum is associated
    with a function value equal to 0.
  tolxabsolute The absolute tolerance on x.
  tolxrelative The relative tolerance on x.
  tolxmethod Possible values: FALSE, TRUE.
  funevals The number of function evaluations.
  maxfunevals The maximum number of function evaluations.
  maxiter The maximum number of iterations.
  iterations The number of iterations.
  fun The cost function.
status  The status of the optimization.

historyfopt  The vector to store the history for fopt. The values of the cost function will be stored at each iteration in a new element, so the length of historyfopt at the end of the optimization should be the number of iterations.

historyxopt  The list to store the history for xopt. The vectors of estimates will be stored on separated levels of the list, so the length of historyfopt at the end of the optimization should be the number of iterations.

verbosetermination  The verbose option for termination criteria.

outputcommand  The command called back for output.

outputcommandarg  The outputcommand argument is initialized as a string. If the user configure this element, it is expected that a matrix of values or a list is passed so that the argument is appended to the name of the function.

numberofvariables  The number of variables to optimize.

storehistory  The flag which enables/disables the storing of the history.

costfargument  The costf argument is initialized as a string. If the user configure this element, it is expected that a matrix of values or a list is passed so that the argument is appended to the name of the function.

boundsmin  Minimum bounds for the parameters.

boundsmax  Maximum bounds for the parameters.

nbineqconst  The number of nonlinear inequality constraints.

logfile  The name of the log file.

logfilehandle  The handle for the log file.

logstartup  Set to TRUE when the logging is started up.

withderivatives  Set to TRUE when the method uses derivatives.

method  The name of the algorithm to use.

simplex0  An object of class 'simplex', i.e. a list created by optim simplex(), and containing the following elements:

verbose  The verbose option, controlling the amount of messages.

x  The coordinates of the vertices, with size nbve x n.

n  The dimension of the space.

fv  The function values, with size nbve x 1.

nbve  The number of vertices.

simplex0method  The method to use to compute the initial simplex.

simplex0length  The length to use when the initial simplex is computed with the 'axes' or 'spendley' methods.

rho  The reflection coefficient. This parameter is used when the method element is set to 'fixed' or 'variable'.

chi  The expansion coefficient. This parameter is used when the method element is set to 'variable'.

gamma  The contraction coefficient. This parameter is used when the method element is set to 'variable'.
sigma: The shrinkage coefficient. This parameter is used when the method element is set to 'fixed' or 'variable'.

tolfstddeviation: The tolerance for the standard deviation.

tolfstddeviationmethod: Set to FALSE.

tolsimplexizeabsolute: The absolute tolerance on the simplex size.

tolsimplexizerelative: The relative tolerance on the simplex size.

tolsimplexizemethod: Logical flag to enable/disable the tolerance on the simplex size. When this criteria is enabled, the values of the tolsimplexizeabsolute and tolsimplexizerelative elements are used in the termination criteria. The method to compute the size is the 'sigmaplus' method.

simplexsize0: Initial size of the simplex, for the tolerance on the simplex size.

toldeltafv: The absolute tolerance on the difference between the highest and the lowest function values.

tolssizedeltafvmethod: Logical flag to enable/disable the termination criteria based on the size of the simplex and the difference of function value in the simplex. If this criteria is triggered, the status of the optimization is set to 'tolsizedeltafv'. This termination criteria uses the values of the tolsimplexizeabsolute and toldeltafv elements. This criteria is identical to Scilab's fminsearch.

historysimplex: The list to store the history for simplex. The simplex will be stored on a new level of the list at each iteration, so the length of historyfopt at the end of the optimization should be the number of iterations.

cords0: The coordinates of the vertices of the initial simplex. If the simplex0method element is set to 'given', these coordinates are used to compute the initial simplex. This matrix is expected to have shape nbve x n where nbve is the number of vertices and n is the number of variables.

simplex0deltausual: The relative delta for non-zero parameters in 'pfeffer' method.

simplex0deltazero: The absolute delta for non-zero parameters in 'pfeffer' method.

simplexopt: The optimum simplex, after one optimization process.

restartsimplexmethod: The method to compute the initial simplex after a restart.

restartmax: The maximum number of restarts, when automatic restart is enabled via the restartflag element.

restarteps: The absolute epsilon value used to check for optimality in the factorial O’Neill restart detection.

restartstep: The absolute step length used to check for optimality in the factorial O’Neill restart detection.
kelleystagnationflag
Logical flag to enable/disable the termination criteria using Kelley’s stagnation
detection, based on sufficient decrease condition. If this criteria is triggered, the
status of the optimization is set to 'kelleystagnation'.

kelleynormalizationflag
Logical flag to enable/disable the normalization of the alpha coefficient in Kel-
ley’s stagnation detection, i.e. use the value of the kelleystagnationalpha0
element as is.

kelleystagnationalpha0
The parameter used in Kelley’s stagnation detection.

kelleyalpha
The current value of Kelley’s alpha, after normalization, if required.

restartnb
Number of restarts performed.

restartflag
Logical flag to enable/disable the automatic restart of the algorithm.

restartdetection
The method to detect if the automatic restart must be performed.

startupflag
Set to TRUE when the startup has been performed.

boxnbpoints
The number of points in the initial simplex, when the simplex0method is set
to 'randbounds’. The value of this element is also use to update the simplex
when a restart is performed and the restartsimplexmethod element is set to
'randbounds’. The default value is so that the number of points is twice the
number of variables of the problem.

boxnbpointseff
The effective number of points required in the simplex for Box’s algorithm.

boxineqscaling
The scaling coefficient used to scale the trial point for function improvement or
into the constraints of Box’s algorithm.

checkcostfunction
Logical flag to enable/disable the checking of the connection of the cost func-
tion.

scalingsimplex0
The algorithm used to scale the initial simplex into the nonlinear constraints.
The following two algorithms are provided:
'tox0' scales the vertices toward the initial guess.
'tocentroid’ scales the vertices toward the centroid, as recommended by Box.

If the centroid happens to be unfeasible, because the constraints are not convex,
the scaling of the initial simplex toward the centroid may fail. Since the initial
guess is always feasible, scaling toward the initial guess cannot fail.

guinalphamin
The minimum value of alpha when scaling the vertices of the simplex into non-
linear constraints in Box’s algorithm.

boxboundsalpha
The parameter used to project the vertices into the bounds in Box’s algorithm.

boxtermination
Logical flag to enable/disable Box’s termination criteria.

boxtolf
The absolute tolerance on difference of function values in the simplex, suggested
by Box. This tolerance is used if the boxtermination element is set to TRUE.

boxnbmatch
The number of consecutive match of Box’s termination criteria.

boxkount
Current number of consecutive match.
boxreflect The reflection factor in Box’s algorithm.
tolvarianceflag Logical flag to enable/disable the termination criteria based on the variance of the function value. If this criteria is triggered, the status of the optimization is set to ‘tolvariance’. This criteria is suggested by Nelder and Mead.
tolabsolutevariance The absolute tolerance on the variance of the function values of the simplex.
tolrelativevariance The relative tolerance on the variance of the function values of the simplex.
variancesimplex0 Relative tolerance on variance.
mymethod A user-defined simplex algorithm.
myterminate A user-defined terminate function.
myterminateflag Logical flag to enable/disable the user-defined terminate function.
greedy Logical flag to enable/disable greedy Nelder-Mead.
output The command to call back for user-defined output of specialized function.
exitflag Logical flag to enable/disable the user-defined output of specialized function.
x An object of class ‘neldermead’.
verbose A logical flag, controlling the amount of data printed.
... optional arguments to ‘print’ or ‘plot’ methods.
object An object of class ‘neldermead’.
showhistory Optional logical flag, to define whether optimization history must be summarized or not.

Value

The neldermead function returns a new object of class ‘neldermead’, with the following default content:

optbase An object of class ‘optimbase’ with the following default content:

verbose Default is FALSE.
x0 Default is NULL.
fx0 Default is NULL.
xopt Default is 0.
fopt Default is 0.
tolfunabsolute Default is 0.
tolfunrelative Default is .Machine$double.eps.
tolfunmethod Default is FALSE.
tolxabsolute Default is 0.
tolxrelative Default is .Machine$double.eps.
tolxmethod Default is TRUE.
funevals Default is 0.
**maxfunevals** Default is 100.
**maxiter** Default is 100.
**iterations** Default is 0.
**fun** Default is ".
**status** Default is ".
**historyfopt** Default is NULL.
**historyxopt** Default is NULL.
**verbosetermination** Default is FALSE.
**outputcommand** Default is ".
**outputcommandarg** Default is ". If the user configures this element, it is expected to be an object of class 'optimbase.outputargs' or will be coerced to an object of class 'optimbase.outputargs'.
**numberofvariables** Default is 0.
**storehistory** Default is FALSE.
**costfargument** Default is ".
**costfargumentarg** If the user configures this element, it is expected to be an object of class 'optimbase.functionargs' or will be coerced to an object of class 'optimbase.functionargs'.
**boundsmin** Default is NULL.
**boundsmax** Default is NULL.
**nbineqconst** Default is 0.
**logfile** Default is ".
**logfilehandle** Default is 0.
**logstartup** Default is FALSE.
**withderivatives** Default is FALSE.
**method** Default is 'variable'.
**simplex0** Default is an object of class 'simplex', with the following content:
  **verbose** Default is 0.
  **x** Default is NULL.
  **n** Default is 0.
  **fv** Default is NULL.
  **nbve** Default is 0.
**simplex0method** Default is 'axes'.
**simplex0length** Default is 1.
**rho** Default is 1.
**chi** Default is 2.
**gamma** Default is 0.5.
**sigma** Default is 0.5.
**tolfstdeviation** Default is 0.
**tolfstdeviationmethod** Default is FALSE.
**tolsimplexsizeabsolute** Default is 0.
**tolsimplexizerelative** Default is .Machine$double.eps.
tolsimplexizemethod Default is FALSE.
simplexsize0 Default is 0.
toldeltafv Default is .Machine$double.eps.
tolssizedeltafvmethod Default is FALSE.
historysimplex Default is NULL.
coords0 Default is NULL.
simplex0deltausual Default is 0.05.
simplex0deltazero Default is 0.0075.
simplexopt Default is NULL.
restartsimplexmethod Default is 'oriented'.
restartmax Default is 3.
restarteps Default is .Machine$double.eps.
restartstep Default is 1.
kelleystagnationflag Default is FALSE.
kelleynormalizationflag Default is TRUE, i.e. the simplex gradient of the initial simplex is taken into account in the stagnation detection.
kelleystagnationalpha0 Default is 1.e-4.
kellyalpha Default is 1.e-4.
restartnb Default is 0.
restartflag Default is FALSE.
restartdetection Default is 'oneill'.
startupflag Default is FALSE.
boxnbpoints Default is '2n'.
boxnbpointseff Default is 0.
boxineqscaling Default is 0.
checkcostfunction Default is TRUE.
scalingsimplex0 Default is 'tox0'.
guinalphamin Default is 1.e-6.
boxtermination Default is FALSE.
boxtolf Default is 1.e-5.
boxnbmatch Default is 5.
boxkount Default is 0.
boxreflect Default is 1.3.
volvarianceflag Default is FALSE.
tolabsolutevariance Default is 0.
tolarelativemcvariance Default is .Machine$double.eps.
variancesimplex0 Default is .Machine$double.eps.
**mymethod** Default is NULL.

**myterminate** Default is NULL.

**myterminateflag** Default is FALSE.

**greedy** Default is FALSE.

**output** Default is list().

**exitflag** Default is FALSE.

### Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

### See Also

`optimbase`, `optimsimplex`

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**neldermead.algo**  
**Nelder-Mead Algorithm**

### Description

`neldermead.algo` performs an optimization without restart using the method associated with the `method` element of the neldermead object; `neldermead.fixed`, `neldermead.variable`, `neldermead.box`, `boxlinesearch`, `neldermead.storehistory`, `neldermead.termination`, and `neldermead.interpolate` are utility functions for `neldermead.algo`.

### Usage

```r
neldermead.algo(this = NULL)  
neldermead.fixed(this = NULL)  
neldermead.variable(this = NULL)  
neldermead.box(this = this)  
boxlinesearch(this = NULL, n = NULL, xbar = NULL, xhigh = NULL, fhigh = NULL, rho = NULL)  
neldermead.storehistory(this = NULL, n = NULL, fopt = NULL, xopt = NULL, fv = NULL, xcoords = NULL)  
neldermead.termination(this = NULL, fvinitial = NULL, oldfvmean = NULL, newfvmean = NULL, previousxopt = NULL, currentxopt = NULL, simplex = NULL)  
neldermead.interpolate(x1 = NULL, x2 = NULL, fac = NULL)
```
Arguments

- **this**: A neldermead object.
- **n**: Number of variables.
- **xbar**: The centroid.
- **xhigh**: The high point.
- **fhigh**: The value of the cost function at xhigh.
- **rho**: The reflection factor.
- **fopt**: The current value of the function at the current optimum point estimate.
- **xopt**: The current optimum point estimate.
- **fv**: The function values, with size nbve x 1.
- **xcoords**: Matrix of size n x n+1, coordinates of the n+1 vertices
- **fvinitial**: The initial cost function value.
- **oldfvmean**: The old cost function value average on the simplex.
- **newfvmean**: The new cost function value average on the simplex.
- **previousxopt**: The previous point estimate.
- **currentxopt**: The current point estimate.
- **simplex**: The simplex. The best point estimate in the simplex is expected to be stored at 1, while the worst point estimate in the simplex is expected to be stored at n+1.
- **x1**: The first reference point estimate to perform the interpolation.
- **x2**: The second reference point estimate to perform the interpolation.
- **fac**: A factor to perform the interpolation.

Details

**neldermead.fixed** The simplex algorithm with fixed size simplex. We implement the following 'rules' of the method of Spendley et al.

- Rule 1 is strictly applied, but the reflection is done by reflection of the high point, since we minimize a function instead of maximizing it, like Spendley.
- Rule 2 is NOT implemented, as we expect that the function evaluation is not subject to errors.
- Rule 3 is applied, i.e. reflection with respect to next to high point. A shrink step is included, with shrinkage factor sigma.

Rule 1. Ascertain the lowest reading y, of yi ... Yk+1 Complete a new simplex Sp by excluding the point Vp corresponding to y, and replacing it by V* defined as above.

Rule 2. If a result has occurred in (k + 1) successive simplexes, and is not then eliminated by application of Rule 1, do not move in the direction indicated by Rule 1, or at all, but discard the result and replace it by a new observation at the same point.

Rule 3. If y is the lowest reading in So , and if the next observation made, y* , is the lowest reading in the new simplex S , do not apply Rule 1 and return to So from Sp . Move out of S, by rejecting the second lowest reading (which is also the second lowest reading in So).

**neldermead.variable** The original Nelder-Mead algorithm, with variable-size simplex.
neldermead.box The Nelder-Mead algorithm, with variable-size simplex and modifications by Box for bounds and inequality constraints.

boxlinesearch Called by neldermead.box, i.e. Box’s method. Perform a line search from xbar, on the line (xhigh,xbar). The reflected point estimate satisfies the following constraints:

- \( f_r < f_{high} \)
- \( x_r \) satisfies the bounds constraints
- \( x_r \) satisfies the nonlinear positive inequality constraints
- \( x_r \) satisfies the linear positive inequality constraints

The method is based on projection and scaling toward the centroid.

neldermead.storehistory Store the optimization history into the neldermead object.

neldermead.termination Determine if the algorithm must continue or terminate. The function uses the cost function average in the simplex instead of the best cost function value. This is because the function average changes at each iteration. Instead, the best function value has a step-by-step evolution and may not change between two successive iterations, leading to a stop of the algorithm.

neldermead.interpolate Compute the point estimate \( x_i \) as an interpolation between \( x_1 \) and \( x_2 \), as follows: \( x_i = (1+fac)x_1 - fac*x_2 \)

Value

neldermead.fixed, neldermead.variable, and neldermead.box Return the updated neldermead object, containing the optimum point estimate.

boxlinesearch Return a list with the following elements:

- **this** The updated neldermead object.
- **status** TRUE if the search is successful, FALSE otherwise.
- **xr** The reflected point estimate.
- **fr** The value of the cost function at \( x_r \).

neldermead.storehistory Return the updated neldermead object.

neldermead.termination Return a list with the following elements:

- **this** The updated neldermead object
- **terminate** TRUE if the algorithm terminates, FALSE if the algorithm must continue.
- **status** The termination status: 'continue', 'maxiter', 'maxfuneval', 'tolf', 'tolx', 'tolsize', 'tolsizedeltafv', 'kelleystagnation', 'tolboxf', 'tolvariance' or the user-defined termination status.

neldermead.interpolate Return a new point estimate, i.e. a column vector.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
neldermead.destroy  Erase a neldermead object.

Description
neldermead.destroy calls optimbase.destroy and optimsimplex.destroy to erase the content of this$optbase and this$simplex0.

Usage
neldermead.destroy(this = NULL)

Arguments
this  A neldermead object.

Value
Return an updated neldermead object.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
optimbase.destroy, optimsimplex.destroy

neldermead.function  Call Cost Function.

Description
Simple way to compute the value of the cost function specified in a neldermead object.

Usage
neldermead.function(this = NULL, x = NULL)

Arguments
this  A neldermead object.
x  The point estimate where the cost function is to be evaluated.
neldermead.get

Value

Returns the value of the cost function.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

neldermead.get Get the value for the given element

Description

Get the value for the given element in a neldermead object.

Usage

neldermead.get(this = NULL, key = NULL)

Arguments

dthis

A neldermead object.

key

The name of the key to query.

Value

Return the value of the list element key, or an error message if key does not exist in the neldermead object this.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

neldermead.set.optimbase.get
neldermead.restart  

Restart neldermead search.

Description

Update the simplex with neldermead.updatesimp and restart the search with neldermead.search.

Usage

neldermead.restart(this = NULL)

Arguments

this A neldermead object.

Value

Returns an updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

neldermead.updatesimp, neldermead.search.

neldermead.search  

Starts the optimization

Description

Performs the optimization associated with the method associated with the method element of the neldermead object and find the optimum. If the restartflag element is enabled, automatic restarts are performed, based on the restartdetection element.

Usage

neldermead.search(this = NULL)

Arguments

this A neldermead object.
Value
Return an updated neldermead object.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
fminsearch, neldermead, neldermead.set.

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neldermead.set  Neldermead Object Configuration

Description
Configure the current neldermead object with the given value for the given key.

Usage
neldermead.set(this = NULL, key = NULL, value = NULL)

Arguments
this  The current neldermead object.
key   The key to configure. See details for the list of possible keys.
value The value to assign to the key.

Details
neldermead.set sets the content of the key element of the neldermead object this to value. If
key is a sub-element of this$optbase, value is assigned by optimbase.set.
The main available keys are the following:
'-verbose'  Set to 1 to enable verbose logging.
'-verbosetermination'  Set to 1 to enable verbose termination logging.
'-x0'  The initial guess, as a n x 1 column vector, where n is the number of variables.
'-maxfunevals'  The maximum number of function evaluations. If this criteria is triggered during
optimization, the status of the optimization is set to 'maxfuneval'.
'-maxiter'  The maximum number of iterations. If this criteria is triggered during optimization, the
status of the optimization is set to 'maxiter'.option
'-tolfunabsolute'  The absolute tolerance for the function value.
'-tolfunrelative'  The relative tolerance for the function value.
'-tolfunmethod' The method used for the tolerance on function value in the termination criteria.
   The following values are available: TRUE, FALSE. If this criteria is triggered, the status of
   the optimization is set to 'tolf'.

'-tolxabsolute' The absolute tolerance on x.

'-tolxrelative' The relative tolerance on x.

'-tolxmethod' The method used for the tolerance on x in the termination criteria. The following
   values are available: TRUE, FALSE. If this criteria is triggered during optimization, the status
   of the optimization is set to 'tolx'.

'-function' The objective function, which computes the value of the cost and the non linear con-
   straints, if any. See vignette('neldermead',package='neldermead') for the details of the
   communication between the optimization system and the cost function.

'-costfargument' An additional argument, passed to the cost function.

'-outputcommand' A command which is called back for output. See vignette('neldermead',package='neldermead')
   for the details of the communication between the optimization system and the output command
   function.

'-outputcommandarg' An additional argument, passed to the output command option

'-numberofvariables' The number of variables to optimize.

'-storehistory' Set to TRUE to enable the history storing.

'-boundsmin' The minimum bounds for the parameters.

'-boundsmax' The maximum bounds for the parameters.

'-nbineqconst' The number of inequality constraints.

'-method' The name of the algorithm to use. The following methods are available:

   'fixed' the fixed simplex shape algorithm of Spendley et al. This algorithm is for uncon-
      strained problems (i.e. bounds and non linear constraints are not taken into account)

   'variable' the variable simplex shape algorithm of Nelder and Mead. This algorithm is for
      unconstrained problems (i.e. bounds and non linear constraints are not taken into account)

   'box' Box's complex algorithm. This algorithm takes into account bounds and nonlinear
      inequality constraints.

   'mine' the user-defined algorithm, associated with the mymethod element. See vignette('neldermead',package='neldermead')
      for details.

'-simplex0method' The method to use to compute the initial simplex. The first vertex in the sim-
   plex is always the initial guess associated with the x0 element. The following methods are
   available:

   'given' The coordinates associated with the coords0 element are used to compute the initial
      simplex, with arbitrary number of vertices. This allows the user to setup the initial
      simplex by a specific method which is not provided by the current package (for example
      with a simplex computed from a design of experiments). This allows also to configure
      the initial simplex so that a specific behaviour of the algorithm is to be reproduced (for
      example the Mac Kinnon test case). The given matrix is expected to have nbve rows and
      n columns, where n is the dimension of the problem and nbve is the number of vertices.

   'axes' The simplex is computed from the coordinate axes and the length associated with the
      simplex0length element.
'spendley' The simplex is computed so that it is regular with the length associated with the
`simplex0length` element (i.e. all the edges have the same length).

'pfeffer' The simplex is computed from an heuristic, in the neighborhood of the initial guess.
This initial simplex depends on the `-simplex0deltausual` and `-simplex0deltazero`.

'randbounds' The simplex is computed from the bounds and a random number. This option
is available only if bounds are available: if bounds are not available, an error is generated.
This method is usually associated with Box’s algorithm. The number of vertices in the
simplex is taken from the `boxnbpoints` element.

'-coords0' The coordinates of the vertices of the initial simplex. If the `simplex0method` element
is set to 'given', these coordinates are used to compute the initial simplex. This matrix is
expected to have shape `nbve x n`, where `nbve` is the number of vertices and `n` is the number of
variables.

'-simplex0length' The length to use when the initial simplex is computed with the 'axes' or 'spend-
ley' methods. If the initial simplex is computed from 'spendley' method, the length is expected
to be a scalar value. If the initial simplex is computed from 'axes' method, it may be either a
scalar value or a vector of values, of length `n`, where `n` is the number of variables.

'-simplex0deltausual' The relative delta for non-zero parameters in 'pfeffer' method.

'-simplex0deltazero' The absolute delta for non-zero parameters in 'pfeffer' method.

'-rho' The reflection coefficient. This parameter is used when the `method` element is set to 'fixed'
or 'variable'.

'-chi' The expansion coefficient. This parameter is used when the `method` element is set to 'vari-
able'.

'-gamma' The contraction coefficient. This parameter is used when the `method` element is set to
'variable'.

'-sigma' The shrinkage coefficient. This parameter is used when the `method` element is set to
'fixed' or 'variable'.

'-tolsimplexizemethod' Set to FALSE to disable the tolerance on the simplex size. If this criteria
is triggered, the status of the optimization is set to 'tolsize'. When this criteria is enabled, the
values of the `tolsimplexizeabsolute` and `tolsimplexizerelative` elements are used in
the termination criteria. The method to compute the size is the 'sigmaplus' method.

'-tolsimplexizeabsolute' The absolute tolerance on the simplex size.

'-tolsimplexizerelative' The relative tolerance on the simplex size.

'-tolssizedeltafvmethod' Set to TRUE to enable the termination criteria based on the size of the
simplex and the difference of function value in the simplex. If this criteria is triggered, the
status of the optimization is set to 'tolsizedeltafv'. This termination criteria uses the values of
the `tolsimplexizeabsolute` and `toldeltafv` elements.

'-toldeltafv' The absolute tolerance on the difference between the highest and the lowest function
values.

'-tolvarianceflag' Set to TRUE to enable the termination criteria based on the variance of the
function value. If this criteria is triggered, the status of the optimization is set to 'tolvariance'.
This criteria is suggested by Nelder and Mead.

'-tolabsolutevariance' The absolute tolerance on the variance of the function values of the sim-
plex.
'-tolrelativevariance' The relative tolerance on the variance of the function values of the simplex.

'-kelleystagnationflag' Set to TRUE to enable the termination criteria using Kelley’s stagnation detection, based on sufficient decrease condition. If this criteria is triggered, the status of the optimization is set to 'kelleystagnation'.

'-kelleynormalizationflag' Set to FALSE to disable the normalization of the alpha coefficient in Kelley’s stagnation detection, i.e. use the value of the kelleystagnationalpha0 element as is. Default value is TRUE, i.e. the simplex gradient of the initial simplex is takeoptionn into account in the stagnation detection.

'-kelleystagnationalpha0' The parameter used in Kelley’s stagnation detection.

'-restartflag' Set to TRUE to enable the automatic restart of the algorithm.

'-restartdetection' The method to detect if the automatic restart must be performed. The following methods are available:

  'oneill' The factorial local optimality test by O’Neill is used. If the test finds a local point which is better than the computed optimum, a restart is performed.

  'kelley' The sufficient decrease condition by O’Neill is used. If the test finds that the status of the optimization is 'kelleystagnation', a restart is performed. This status may be generated if the -kelleystagnationflag option is set to TRUE.

'-restartmax' The maximum number of restarts, when automatic restart is enabled via the -restartflag option.

'-restarteps' The absolute epsilon value used to check for optimality in the factorial O’Neill restart detection.

'-restartstep' The absolute step length used to check for optimality in the factorial O’Neill restart detection.

'-restartsimplexmethod' The method to compute the initial simplex after a restart. The following methods are available.

  'given' The coordinates associated with the coords0 element are used to compute the initial simplex, with arbitrary number of vertices. This allow the user to setup the initial simplex by a specific method which is not provided by the current package (for example with a simplex computed from a design of experiments). This allows also to configure the initial simplex so that a specific behaviour of the algorithm is to be reproduced (for example the Mc Kinnon test case). The given matrix is expected to have nbve rows and n columns, where n is the dimension of the problem and nbve is the number of vertices.

  'axes' The simplex is computed from the coordinate axes and the length associated with the -simplex0length option.

  'spendley' The simplex is computed so that it is regular with the length associated with the -simplex0length option (i.e. all the edges have the same length).

  'pfeffer' The simplex is computed from an heuristic, in the neighborhood of the initial guess. This initial simplex depends on the -simplex0deltausual and -simplex0deltazero.

  'randbounds' The simplex is computed from the bounds and a random number. This option is available only if bounds are available: if bounds are not available, an error is generated. This method is usually associated with Box’s algorithm. The number of vertices in the simplex is taken from the -boxnbpoints option.

  'oriented' The simplex is computed so that it is oriented, as suggested by Kelley.

'-scalingsimplex0' The algorithm used to scale the initial simplex into the nonlinear constraints. The following two algorithms are provided:
'tox0' scales the vertices toward the initial guess.
'tocentroid' scales the vertices toward the centroid, as recommended by Box.

If the centroid happens to be unfeasible, because the constraints are not convex, the scaling of the initial simplex toward the centroid may fail. Since the initial guess is always feasible, scaling toward the initial guess cannot fail.

'-boxnbpoints' The number of points in the initial simplex, when the -simplex0method is set to 'randbounds'. The value of this option is also used to update the simplex when a restart is performed and the -restartsimplexmethod option is set to 'randbounds'. The default value is so that the number of points is twice the number of variables of the problem.

'-boxineqscaling' The scaling coefficient used to scale the trial point for function improvement or into the constraints of Box's algorithm.

'-guinalphamin' The minimum value of alpha when scaling the vertices of the simplex into non-linear constraints in Box's algorithm.

'-boxreflect' The reflection factor in Box's algorithm.

'-boxtermination' Set to TRUE to enable Box's termination criteria.

'-boxtolf' The absolute tolerance on difference of function values in the simplex, suggested by Box. This tolerance is used if the -boxtermination element is set to TRUE.

'-boxnbmatch' The number of consecutive match of Box's termination criteria.

'-boxboundsalpha' The parameter used to project the vertices into the bounds in Box's algorithm.

'-mymethod' A user-defined simplex algorithm. See vignette('neldermead',package='neldermead') for details.

'-myterminate' A user-defined terminate function. See vignette('neldermead',package='neldermead') for details.

'-myterminateflag' Set to TRUE to enable the user-defined terminate function.

Value
An updated neldermead object.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
neldermead
optimget

Queries an optimization option list

Description

This function allows to make queries on an existing optimization option list. This list must have been created and updated by the `optimset` function. The `optimget` allows to retrieve the value associated with a given key.

Usage

```r
optimget(options = NULL, key = NULL, value = NULL)
```

Arguments

- `options` A list created or modifies by `optimset`.
- `key` A single character string, which should be the name of the field in `options` to query (case insensitive).
- `value` A default value.

Details

`key` is matched against the field names of `options` using `grep` and a case-insensitive regular expression. If `key` is not found in `options`, the function returns NULL. If several matches are found, `optimget` is stopped.

Value

Return `options$key` if `key` is found in `options`. Return `value`, otherwise.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

- `optimset`

Examples

```r
opt <- optimset(method='fminsearch')
optimget(opt,'Display')
optimget(opt,'abc','!@')
```
optimset

Configures and returns an optimization data structure.

Description
This function creates or updates a list which can be used to modify the behaviour of optimization methods. The goal of this function is to manage the options list with a set of fields (for example, 'MaxFunEvals', 'MaxIter', etc...). The user can create a new list with empty fields or create a new structure with default fields which correspond to a particular algorithm. The user can also configure each field and set it to a particular value. Finally, the user passes the list to an optimization function so that the algorithm uses the options configured by the user.

Usage
optimset(method = NULL,...)

Arguments
method
If provided, the method calls the optimset.method function. If the content of method is recognized, a default set of options are returned. The only current recognized character strings are 'fminsearch' and 'fminbnd'.

... Additional arguments which would be included in the options output if the method argument is not used. See Details.

Details
Most optimization algorithms require many algorithmic parameters such as the number of iterations or the number of function evaluations. If these parameters are given to the optimization function as input parameters, this forces both the user and the developer to manage many input parameters. The goal of the optimset function is to simplify the management of input arguments, by gathering all the parameters into a single list.

While the current implementation of the optimset function only supports the fminsearch and fminbnd function, it is designed to be extended to as many optimization function as required. Because all optimization algorithms do not require the same parameters, the data structure aims at remaining flexible. But, most of the time, most parameters are the same from algorithm to algorithm, for example, the tolerance parameters which drive the termination criteria are often the same, even if the termination criteria itself is not the same.

Optimization parameters that are returned by the optimset function and that can be defined in ... are the following:

Display The verbose level. The default value is 'notify'. The following is a list of available verbose levels.

'off' The algorithm displays no message at all.

'notify' The algorithm displays message if the termination criteria is not reached at the end of the optimization. This may happen if the maximum number or iterations of the maximum number of function evaluations is reached and warns the user of a convergence problem.
'final'  The algorithm displays a message at the end of the optimization, showing the number of iterations, the number of function evaluations and the status of the optimization. This option includes the messages generated by the 'notify' option i.e. warns in case of a convergence problem.

'iter'  The algorithm displays a one-line message at each iteration. This option includes the messages generated by the 'notify' option i.e. warns in case of a convergence problem. It also includes the message generated by the 'final' option.

FunValCheck  A logical flag to enable the checking of function values.

MaxFunEvals  The maximum number of evaluations of the cost function.

MaxIter  The maximum number of iterations.

OutputFcn  A function which is called at each iteration to print out intermediate state of the optimization algorithm (for example into a log file).

PlotFcns  A function which is called at each iteration to plot the intermediate state of the optimization algorithm (for example into a 2D graphic).

TolFun  The absolute tolerance on function value.

TolX  The absolute tolerance on the variable x.

nbMatch  Specific to Box method: the number of consecutive times the TolFun criteria must be met to terminate the optimization.

boundsAlpha  Specific to Box method: the parameter used to project the vertices into the bounds in Box’s algorithm.

boxScaling  Specific to Box method: the scaling coefficient used to scale the trial point for function improvement or into the constraints of Box’s algorithm.

alphaMin  Specific to Box method: the minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box’s algorithm.

Output and plot functions  The 'OutputFcn' and 'PlotFcns' options accept as argument a function (or a list of functions). In the client optimization algorithm, this output or plot function is called back once per iteration. It can be used by the user to display a message in the console, write into a file, etc... The output or plot function is expected to have the following definition:

myfun <- function(x, optimValues, state)

where the input parameters are:

x  The current point estimate.

optimValues  A list which contains the following fields:

  funccount  The number of function evaluations.

  fval  The best function value.

  iteration  The current iteration number.

  procedure  The type of step performed. This string depends on the specific algorithm (see fminsearch for details).

state  the state of the algorithm. The following states are available:

  'init'  when the algorithm is initializing,

  'iter'  when the algorithm is performing iterations,

  'done'  when the algorithm is terminated.
optimset.method

Value
Return a list with the following fields: Display, FunValCheck, MaxFunEvals, MaxIter, OutputFcn, PlotFcns, TolFun, TolX, nbMatch, boundsAlpha, boxScaling, and alphaMin.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
optimset.method, fminsearch, fminbnd

Examples
optimset()
optimset(Display='iter')
optimset(method='fminbnd')

optimset.method Default set of optimization options

Description
This function returns a default set of optimization options for defined 'methods'; optimset.method is called by optimset when a method was provided as input. Currently, the only valid method is 'fminsearch'.

Usage
optimset.method(method = NULL)

Arguments
method A character string.

Value
Returns a list with the following fields: Display, FunValCheck, MaxFunEvals, MaxIter, OutputFcn, PlotFcns, TolFun, and TolX.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
Secondary search functions

See Also

optimset

Examples

optimset.method('fminsearch')
  # Will fail
  try(optimset.method('abc'))

Description

Utility functions for neldermead.search and dependent functions.

Usage

neldermead.startup(this = NULL)
neldermead.log(this = NULL, msg = NULL)
neldermead.scaletox0(this = NULL, simplex0 = NULL)
neldermead.scaletocenter(this = NULL, simplex0 = NULL, x0 = NULL)
neldermead.termstartup(this = NULL)
neldermead.outputcmd(this = NULL, state = NULL, simplex = NULL, step = NULL)
neldermead.autorestart(this = NULL)
neldermead.istorestart(this = NULL)
neldermead.isroneill(this = NULL)
neldermead.isrkelley(this = this)
neldermead.updatesimp(this = NULL)
scaleinconstraints(this = NULL, x = NULL, xref = NULL)
neldermead.costf(x = NULL, this = NULL)

Arguments

this  A neldermead object.
msg   A character string.
simplex0  The initial simplex object.
x0    A column matrix of initial parameters.
state The state of the algorithm, either 'init', 'done' or 'iter'.
simplex The current simplex object.
step   The type of step performed during the iteration: 'init', 'done', 'reflection', 'expansion', 'insidecontraction', 'outsidecontraction', 'reflectionnext' or 'shrink'.
x     The point estimate to scale.
xref  The reference point estimate.
Details

neldermead.startup  Startup the algorithm. Compute the initial simplex, depending on the content of the simplexmethod element of the neldermead object (‘given’, ‘axes’, ‘spendley’, ‘pfeffer’ or ‘randbounds’).
neldermead.log  Print a message to the log file using optimbase.log.
neldermead.scaletox0  Scale the simplex into the nonlinear inequality constraints, if any. Scale toward x0, which is feasible.
neldermead.scaletocenter  Scale the simplex into the nonlinear inequality constraints, if any. Scale to the centroid of the points which satisfy the constraints. This is Box’s method for scaling. It is unsure, since the centroid of the points which satisfy the constraints may not be feasible.
neldermead.termstartup  Initialize Kelley’s stagnation detection system when normalization is required, by computing kelleyalpha. If the simplex gradient is zero, then use alpha0 as alpha.
neldermead.outputcmd  Call the array of user-defined output functions
neldermead.autorestart  Perform an optimization with automatic restart. The loop processes for i = 1 to restartmax + 1. This is because a RE-start is performed after one simulation has been performed, hence the ’RE’.
neldermead.istorestart  Determine if the optimization is to restart using neldermead.isroneill or neldermead.isrkelley depending on the content of the restartdetection element.
neldermead.isroneill  Determine if the optimization is to restart. Use O’Neill method as a criteria for restart. It is an axis-by-axis search for optimality.
neldermead.isrkelley  Determine if the optimization is to restart. Use kelleystagnation as a criteria for restart.
neldermead.updatesimp  Update the initial simplex simplex0 for a restart.
scaleinconstraints  Given a point reference to scale and a reference point which satisfies the constraints, scale the point towards the reference point estimate until it satisfies all the constraints.
neldermead.costf  Call the cost function and return the value. This function is given to the simplex function class as a callback. Input/Output arguments are swapped w.r.t. optimbase.function, so that it matches the requirements of simplex methods.

Value

neldermead.startup  Return an updated neldermead object this.
neldermead.log  Return the neldermead object this.
neldermead.scaletox0  Return an updated simplex.
neldermead.scaletocenter  Return an updated simplex.
neldermead.termstartup  Return an updated neldermead object this.
neldermead.outputcmd  Do not return any data, but execute the output function(s).
neldermead.autorestart  Return an updated neldermead object this.
neldermead.istorestart  Return a list with the following elements:

  this  The input neldermead object.
**Secondary search functions**

*istorestart* Set to TRUE if the optimization is to restart, to FALSE otherwise.

**neldermead.isroneill** Return a list with the following elements:

- **this** The input neldermead object.
- **istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.

**neldermead.isrkelley** Return a list with the following elements:

- **this** The input neldermead object.
- **istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.

**neldermead.updatesimp** Return an updated neldermead object **this**.

**scaleinconstraints** Return a list with the following elements:

- **this** The updated neldermead object.
- **isscaled** TRUE if the procedure has succeeded before boxnb1lloops, FALSE if it has failed.
- **p** The scaled parameters.

**neldermead.costf** Return a list with the following elements:

- **f** The value of the cost function.
- **this** The updated neldermead object.

**Author(s)**

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sébastien Bihorel (<sb.pmlab@gmail.com>)
Index

* method
  costf.transposex, 5
  fmin.gridsearch, 5
  fminbnd, 6
  fminbnd.function, 9
  fminbnd.outputfun, 10
  fminsearch, 11
  fminsearch.function, 15
  fminsearch.outputfun, 16
  neldermead, 17
  neldermead.algo, 25
  neldermead.destroy, 28
  neldermead.function, 28
  neldermead.get, 29
  neldermead.restart, 30
  neldermead.search, 30
  neldermead.set, 31
  optimget, 36
  optimset, 37
  optimset.method, 39
  Secondary search functions, 40

* package
  neldermead-package, 2
  boxlinesearch (neldermead.algo), 25
  costf.transposex, 5
  fmin.gridsearch, 5
  fminbnd, 6, 10, 11, 39
  fminbnd.function, 9
  fminbnd.outputfun, 10
  fminsearch, 6, 11, 16, 17, 31, 39
  fminsearch.function, 15
  fminsearch.outputfun, 16
  is.neldermead (neldermead), 17
  neldermead, 10, 11, 14, 16, 17, 17, 31, 35
  neldermead-package, 2
  neldermead.algo, 25
  neldermead.autorestart (Secondary search functions), 40
  neldermead.box (neldermead.algo), 25
  neldermead.costf (Secondary search functions), 40
  neldermead.destroy, 28
  neldermead.fixed (neldermead.algo), 25
  neldermead.function, 28
  neldermead.get, 29
  neldermead.interpolate (neldermead.algo), 25
  neldermead.isrkkelley (Secondary search functions), 40
  neldermead.isroneill (Secondary search functions), 40
  neldermead.istorestart (Secondary search functions), 40
  neldermead.log (Secondary search functions), 40
  neldermead.outputcmd (Secondary search functions), 40
  neldermead.restart, 30
  neldermead.scaletocenter (Secondary search functions), 40
  neldermead.scaletox0 (Secondary search functions), 40
  neldermead.search, 30, 30
  neldermead.set, 10, 11, 16, 17, 29, 31, 31
  neldermead.startup (Secondary search functions), 40
  neldermead.storehistory (neldermead.algo), 25
  neldermead.termination (neldermead.algo), 25
  neldermead.termmstartup (Secondary search functions), 40
  neldermead.updatesimp, 30
  neldermead.updatesimp (Secondary search functions), 40
neldermead_variable (neldermead.algo), 25

optimbase, 4, 25
optimbase.destroy, 28
optimbase.get, 29
optimbase.gridsearch, 6
optimget, 36
optimset, 9, 14, 36, 37, 40
optimset.method, 39, 39
optimsimplex, 4, 25
optimsimplex.destroy, 28

print.neldermead (neldermead), 17

scaleinconstraints (Secondary search functions), 40
Secondary search functions, 40
summary.neldermead (neldermead), 17